

Planar Tunneling and Andreev Reflection: Powerful probes of the superconducting order parameter

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UCSB

Outline:

Lecture 1 (Tunneling spectroscopy on HTS):

- **Promo:** Grand statement / DoE-BES report / new SCs
- **Broken symmetries** (gauge, reflection and time-reversal)
- **Tunneling** and order parameter (OP) symmetry
- **Andreev reflection** (AR)
- **Tunneling** into Andreev bound states: Broken symmetries

Lecture 2 (Andreev reflection spectroscopy on HFs):

- Point Contact Andreev Reflection Tunneling Spectroscopy (PCARTS)
- Blonder-Tinkham-Klapwijk (BTK) theory and its extension to d-wave
- Definition of the issues (AR at HFSs and spectroscopy of HFs)
- CeCoIn5 and related HFs
- Describe data with a two-fluid model and Fano resonance in an energy-dependent Dos

History of the Universe

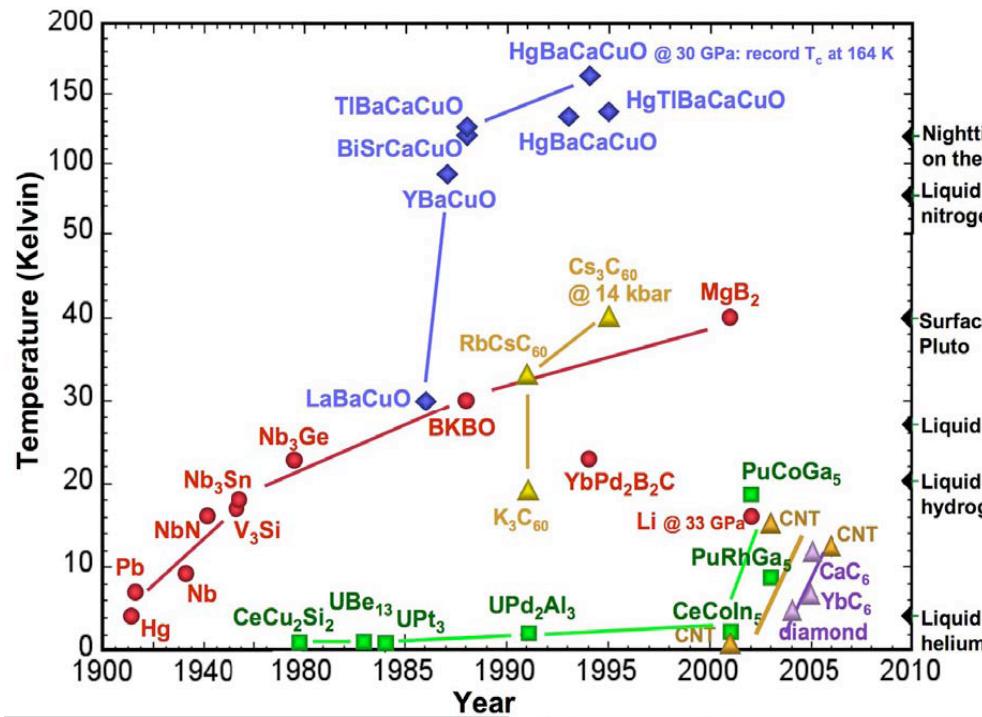
Conditions \sim 10ms after the Big Bang:

- 10 GeV/fm^3 or $\sim 10^{16} \text{ gm/cm}^3$
- $T \sim 170 \text{ MeV}$ or $\sim 2 \times 10^{12} \text{ K}$

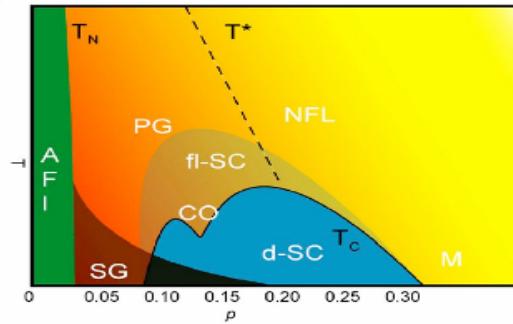
Same physics as superconductivity,
(strongly-correlated Fermion systems)
but $\sim 10^{16}$ difference in energy !



Our 2006 REPORT (with “T_c vs. Time”)



Includes HOW
to search for the
next HTS:

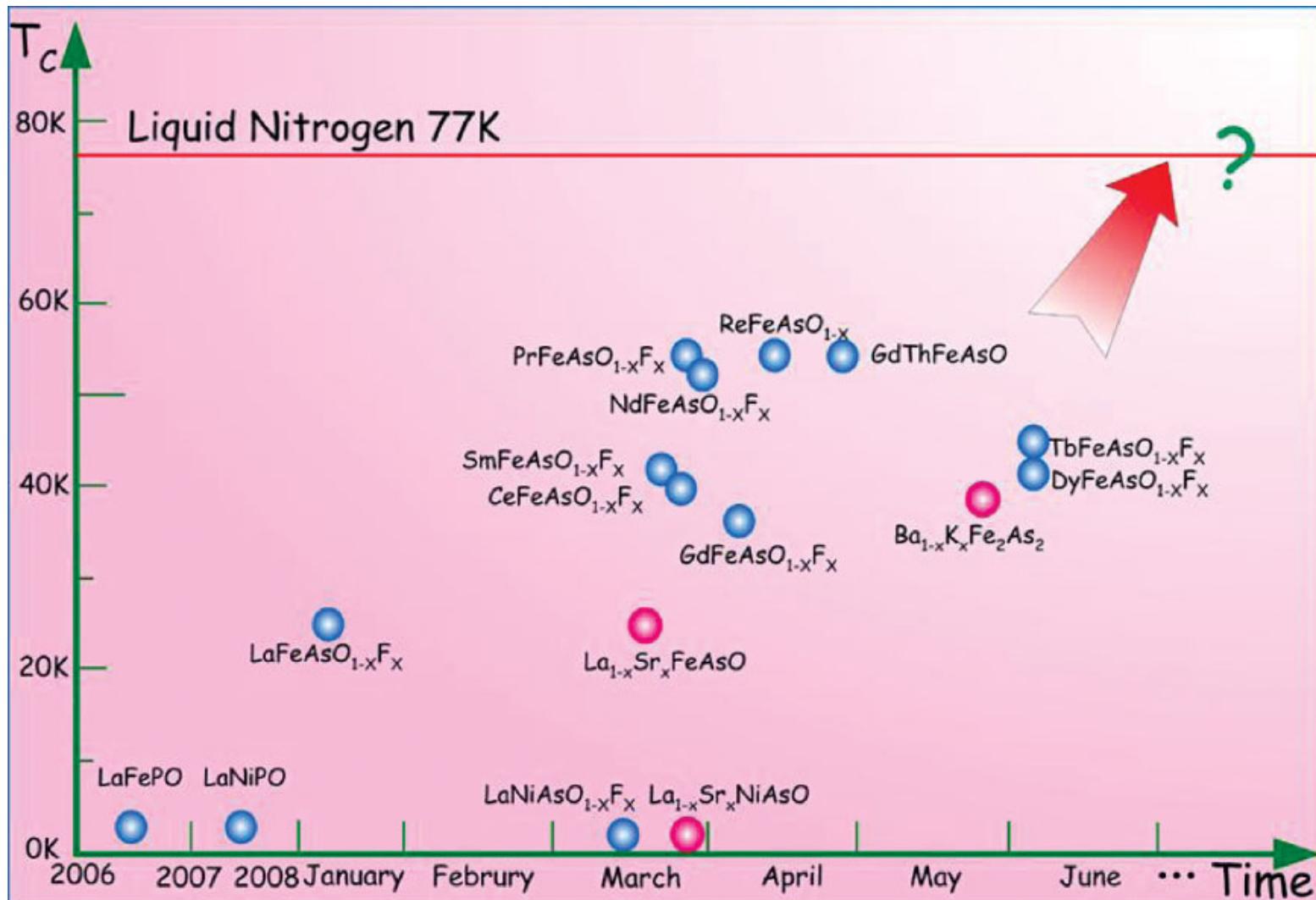


BASIC RESEARCH NEEDS FOR SUPERCONDUCTIVITY

Report of the Basic Energy Sciences
Workshop on Superconductivity,
May 8-11, 2006

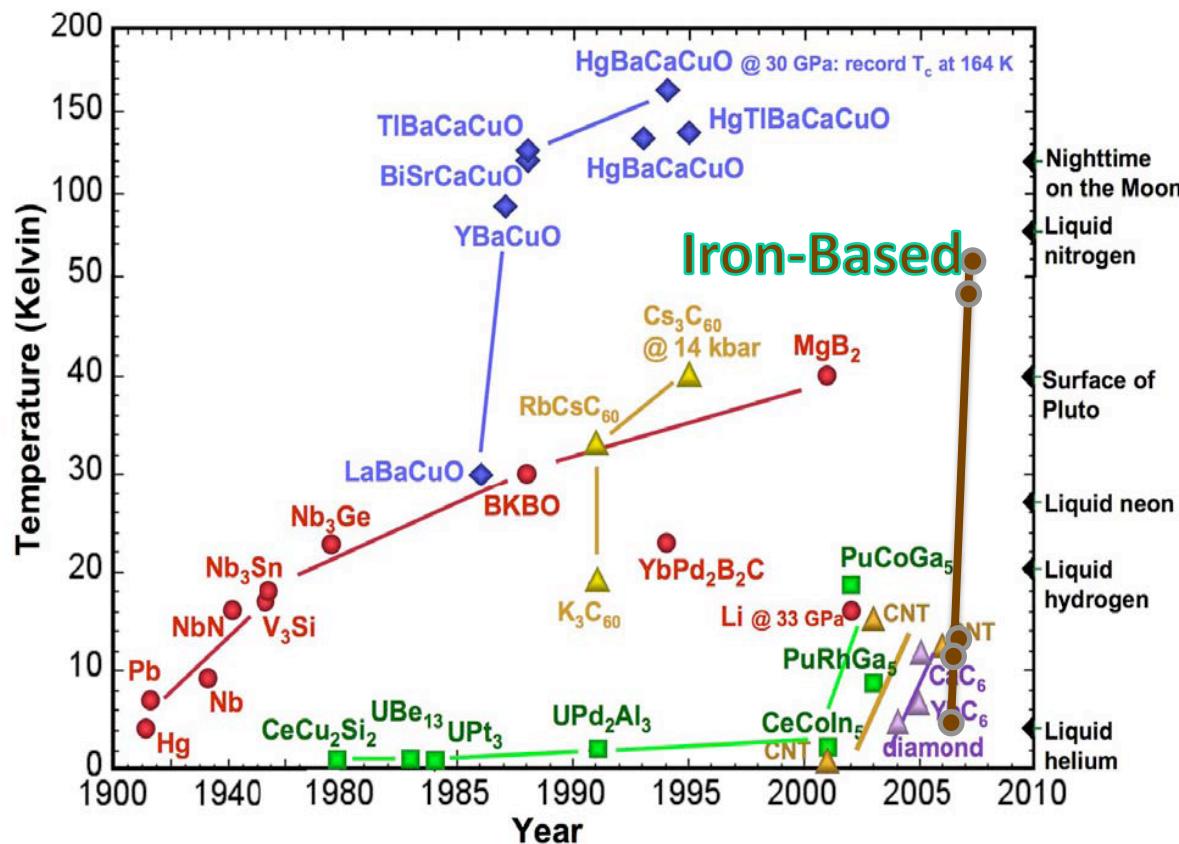
2008 Surprise

Iron-based HTS !!!



Today's "T_c vs. Time" with NEW HTS

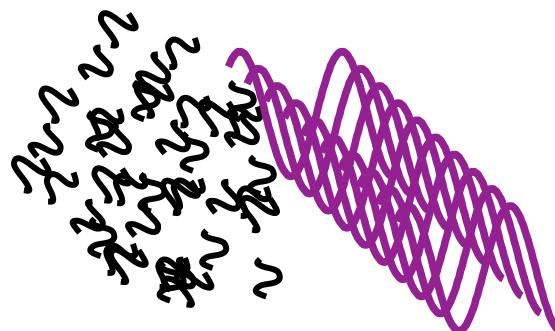
The First HTS are NOT UNIQUE!!!



A SECOND class
of HTS found, so
there MUST be
a THIRD!?

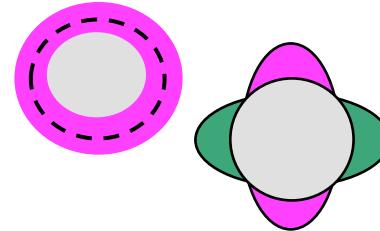
Broken Symmetries - 1 (overview)

High-temperature (and any unconventional) superconductors are playgrounds for broken symmetries



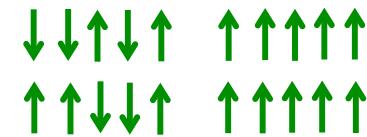
Gauge / Phase

Superconductivity



Reflection

d-wave



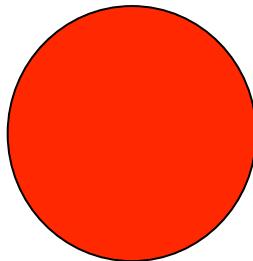
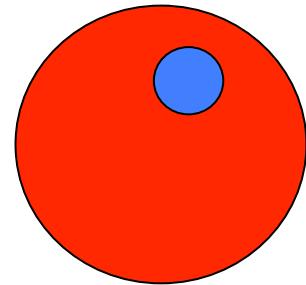
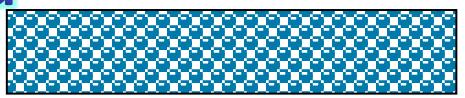
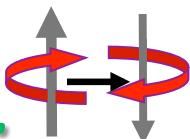
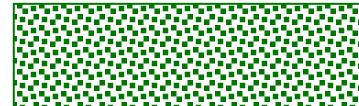
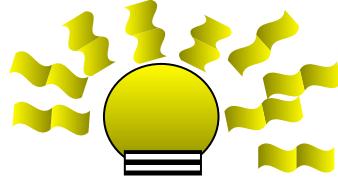
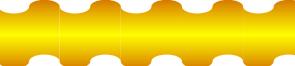
Time Reversal

Ferromagnetism

Broken Symmetries – 2 (definitions)

<i>Symmetry State</i>	<i>Broken Symmetry State</i>
1. <u>Homogeneous</u> w.r.t. coordinate <i>(distance, angle, phase, time, ..)</i>	<u>Inhomogeneous</u> w.r.t. coordinate
2. <i>The symmetry of the state is the <u>same as</u> that of the Hamiltonian</i>	<i>The symmetry of the state is <u>lower</u> than that of the Hamiltonian</i> .
3. <i>Changing the coordinate <u>does not</u> produce a measurable change</i>	<i>Changing a coordinate <u>does</u> produce a measurable change</i>

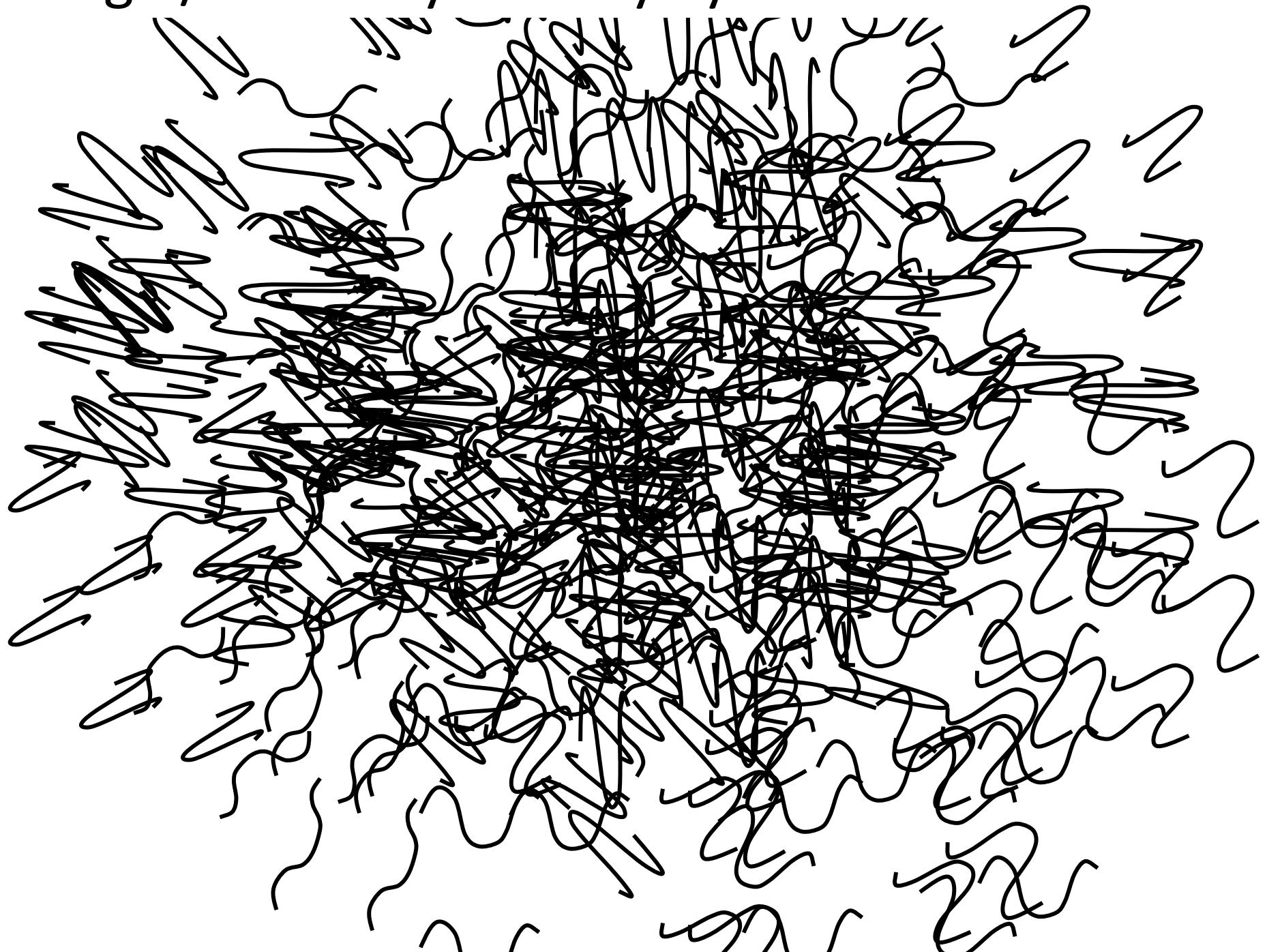
Broken Symmetries – 3: Symmetry vs. Broken Symmetry

Symmetry:	Symmetry State	Broken Symmetry	
Circular			
Translational:	Fluid	Solid	
			
Time Reversal:		Paramagnet	Ferromagnet
			
spontaneous	Metal	Superconductor	
Phase / Gauge			
driven	Light bulb	Laser	
			

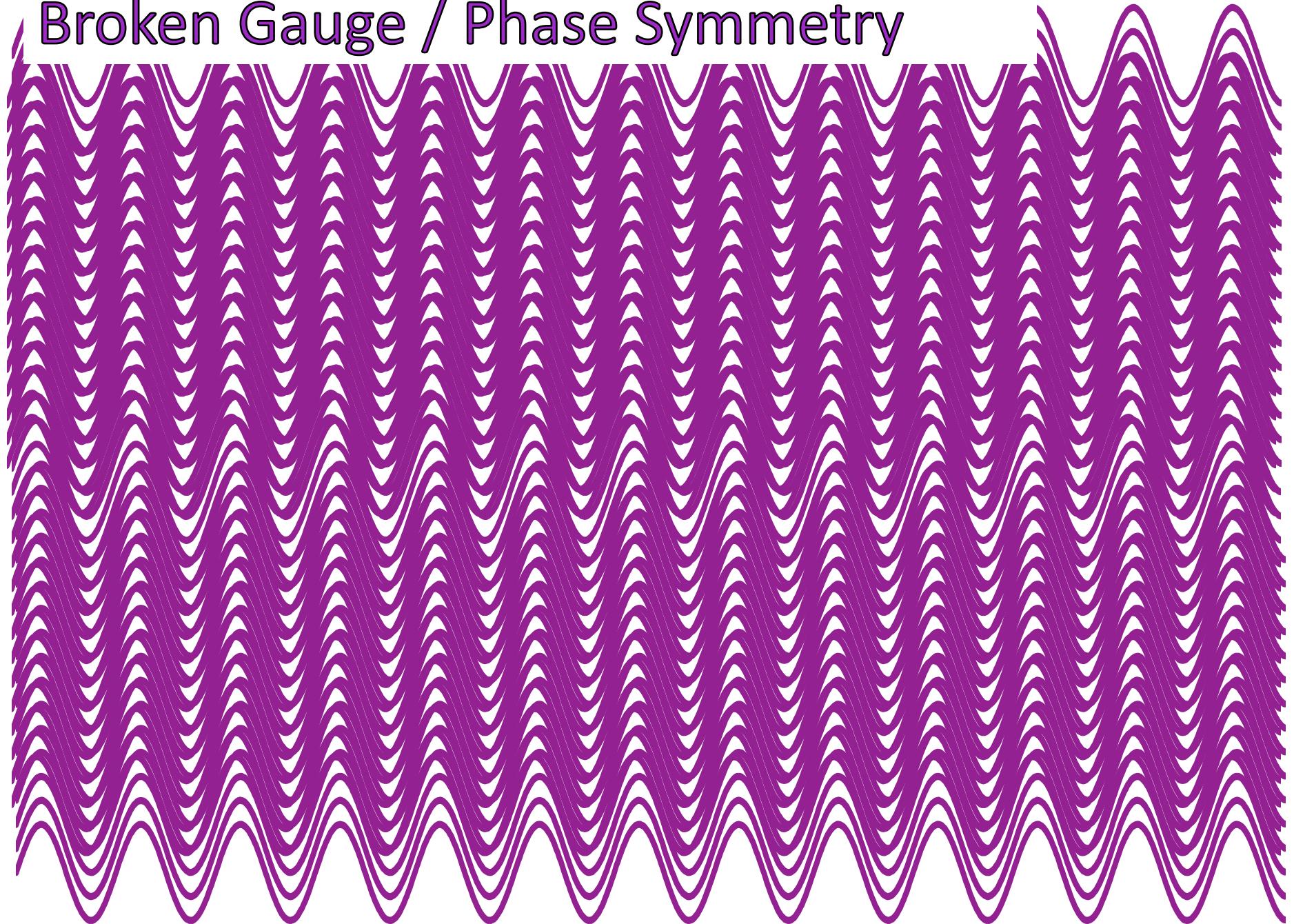
Broken Time-Reversal Symmetry



Gauge / Phase Symmetry Symmetric



Broken Gauge / Phase Symmetry



Broken Symmetries – 4 (some ramifications of broken gauge symmetry)

Photons (driven)

Single-Slit Diffraction:

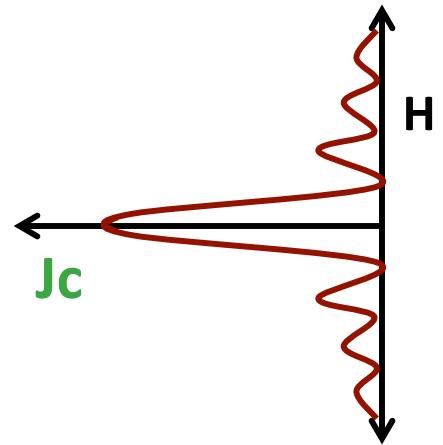
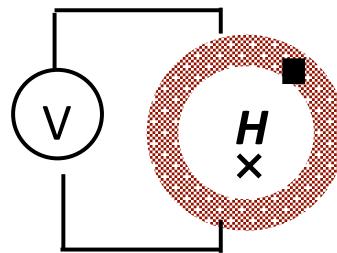
Intensity

Double-Slit Diffraction:

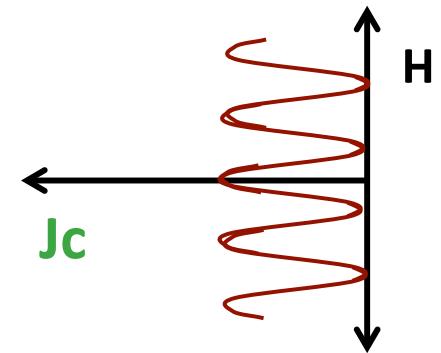
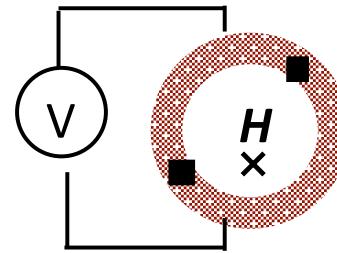
Intensity

Electrons (spontaneous)

rf Squid:

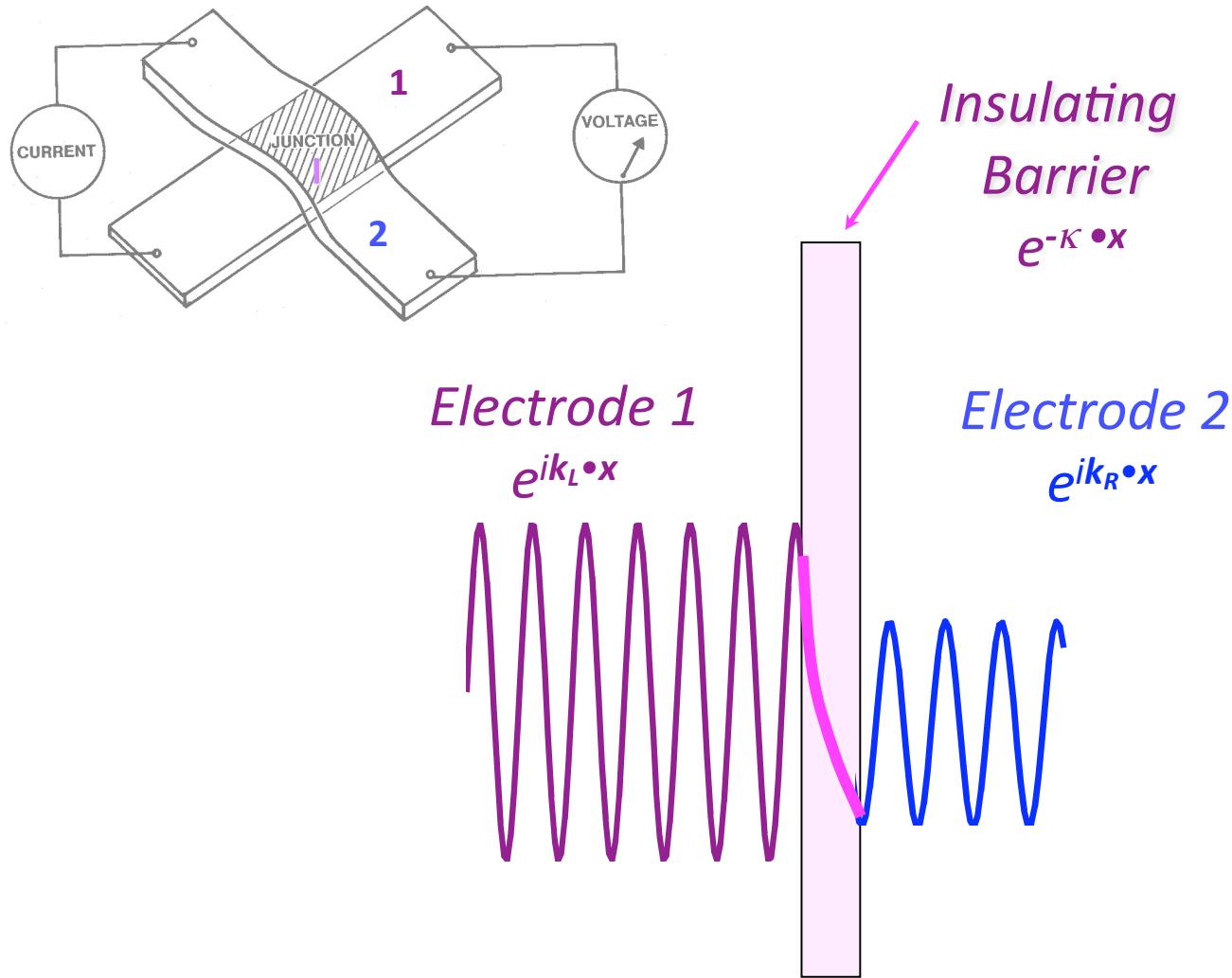


dc Squid:



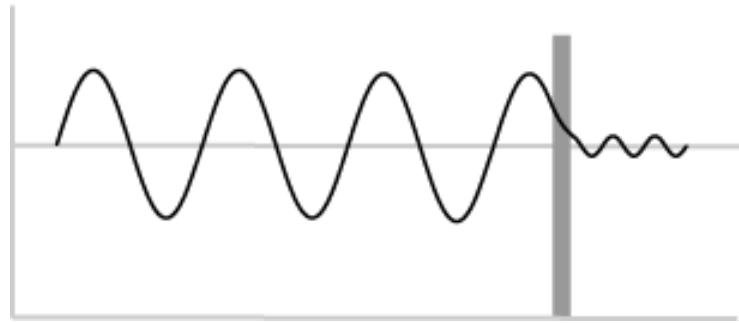
Electron Tunneling Spectroscopy (I)

(Planar quasiparticle overview)

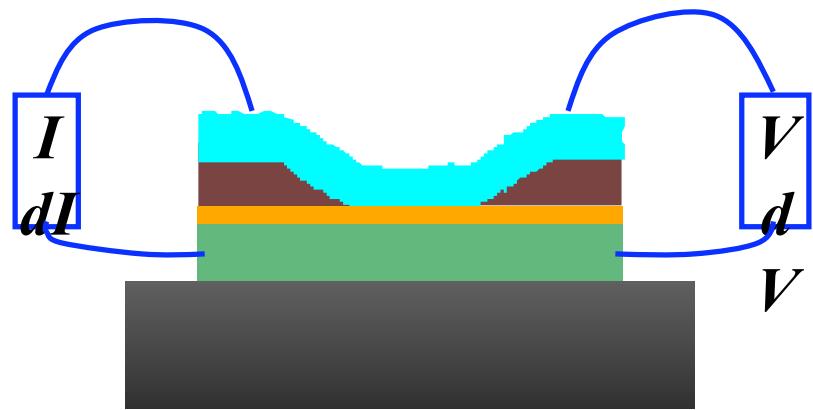


Electron Tunneling Spectroscopy (II)

Quantum Mechanical
Tunneling



Planar Tunnel Junction



- █ Normal metal
- █ Insulator
- █ Tunnel barrier
- █ Superconductor
- █ Substrate

Al/AlO_x/Pb, Giaever (PRL 5 147, 1960)

Electron Tunneling Spectroscopy (III)

Tunnel Current: $I(V) = A |T|^2 e N_n(0) \int_{-\infty}^{\infty} N_s(E) [f(E - eV) - f(E)] dE$

Tunnel Conductance: $G(V) \equiv \frac{dI}{dV} = A |T|^2 e^2 N_n(0) \int_{-\infty}^{\infty} N_s(E) \frac{\partial f(E - eV)}{\partial(eV)} dE$

Tunneling matrix element: $|T|^2 \propto e^{-2\kappa d}$, $\kappa = \left[\left(2m / \hbar^2 \right) (U - \varepsilon_z) \right]^{1/2}$

$$f(E) = \frac{1}{\exp(E/k_B T) + 1}, \text{ Fermi function}$$

For $T = 0$, $\frac{\partial f(E - eV)}{\partial(eV)} = \delta(E - eV) \Rightarrow G(V) \propto N_s(eV).$

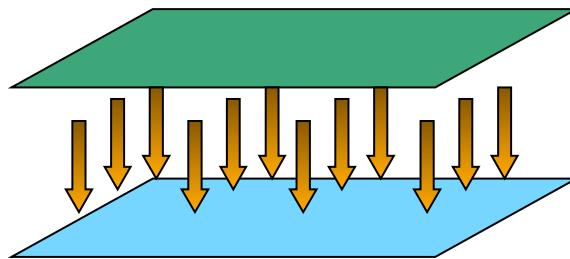
For $T > 0$, $G(V)$ is given as a convolution of SC DOS w.r.t. derivative of Fermi function.

Electron Tunneling Spectroscopy (IV)

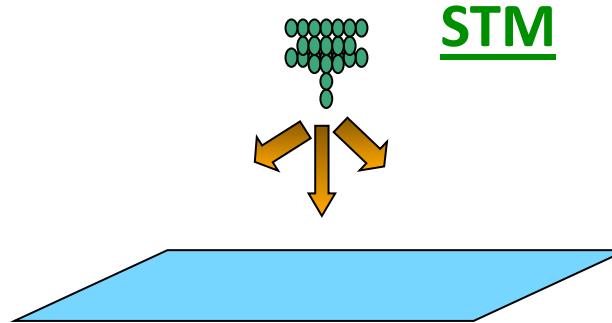
(Planar vs. STM)

Measurements compliment each other:

Planar Tunneling



STM



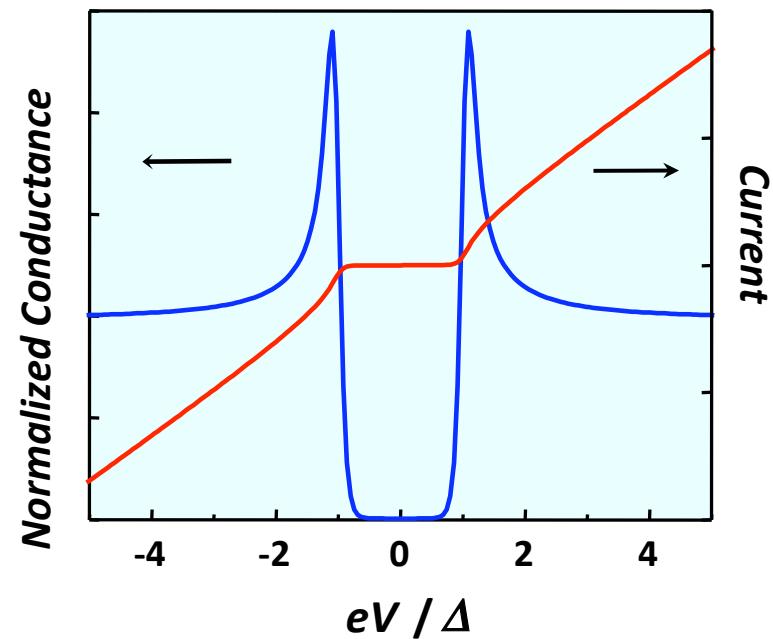
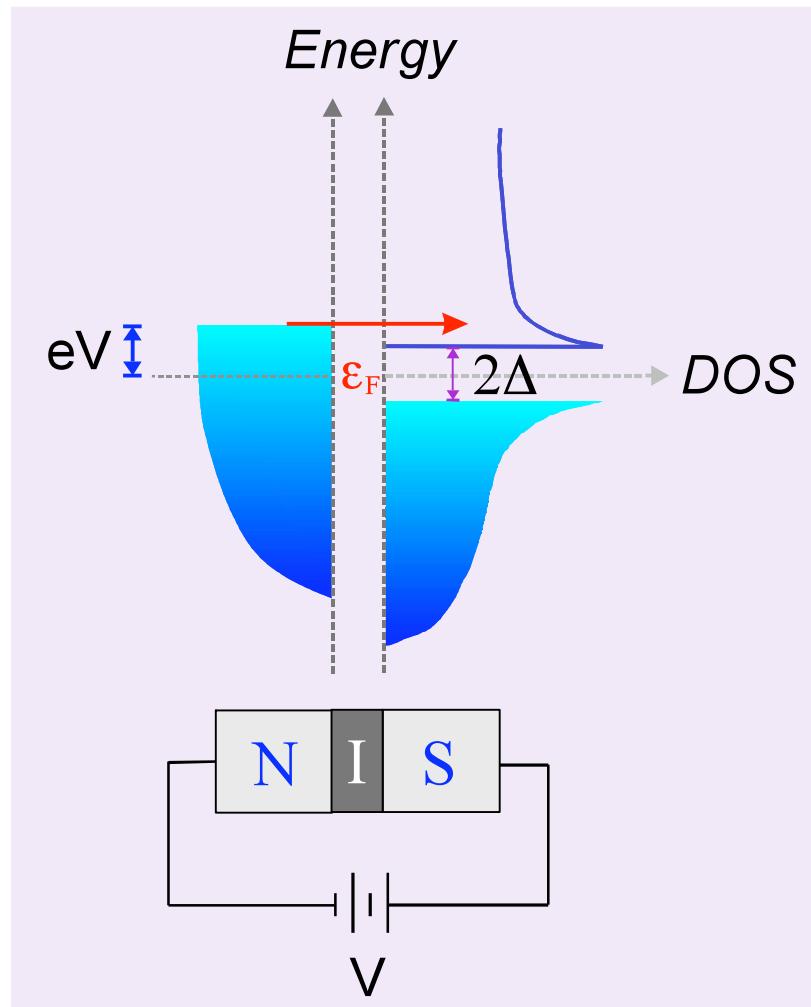
Advantages:

- I. Small tunneling cone:
Intrinsic momentum resolution for smooth surfaces
- II. Stable configuration:
can easily study as a function of field, temperature,
area and, most important, reproducibility.

Drawbacks:

- I. Damage to surface during junction fabrication
- II. Low spatial resolution

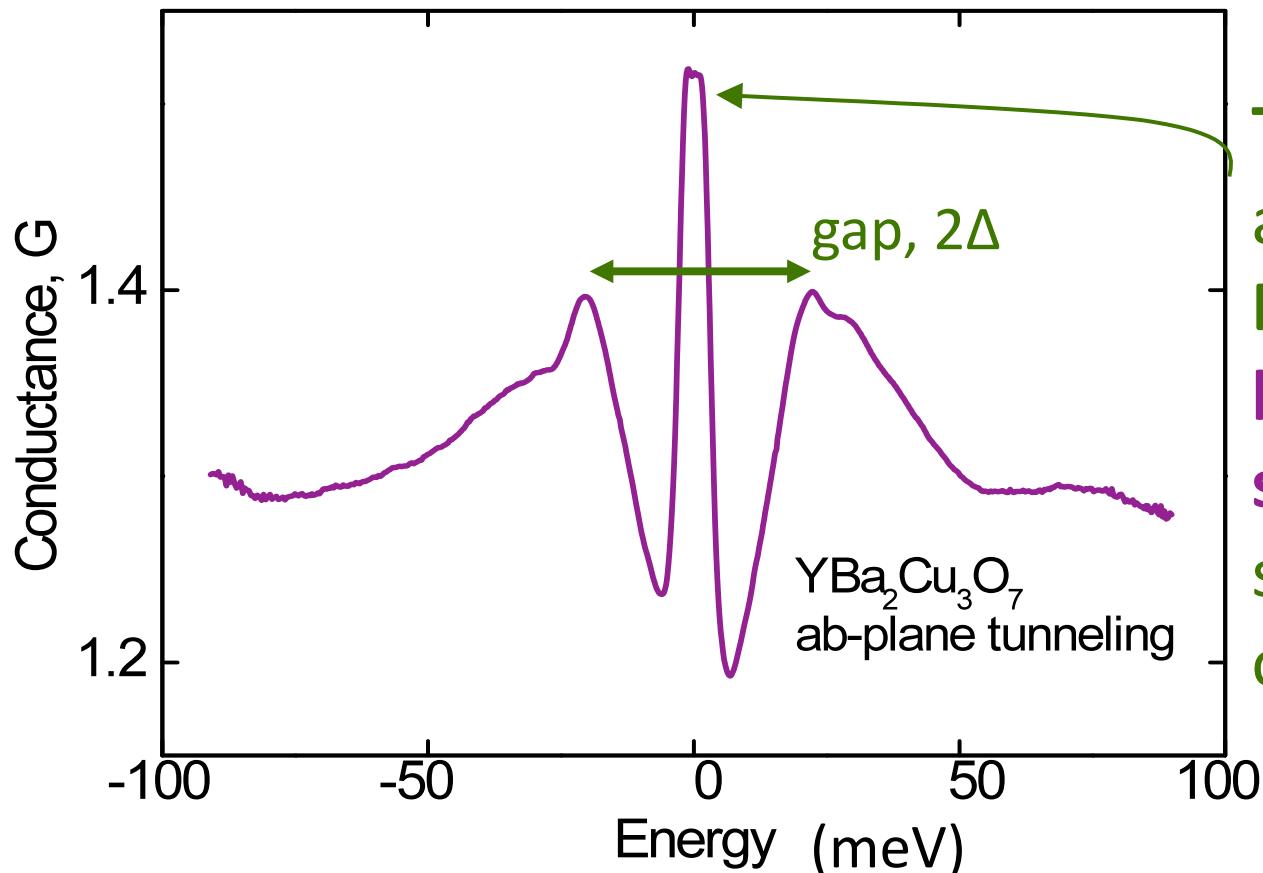
Electron Tunneling Spectroscopy (V)



- Bias dependence of tunneling conductance directly probes DOS.
- Tunneling is a well-established technique to study SC energy gap.

Electron Tunneling Spectroscopy (VI)

Measured Tunneling Conductance of a High-Temperature Superconductor

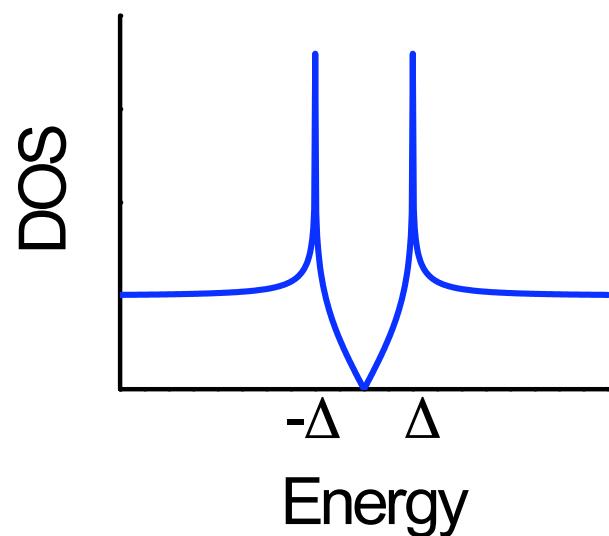
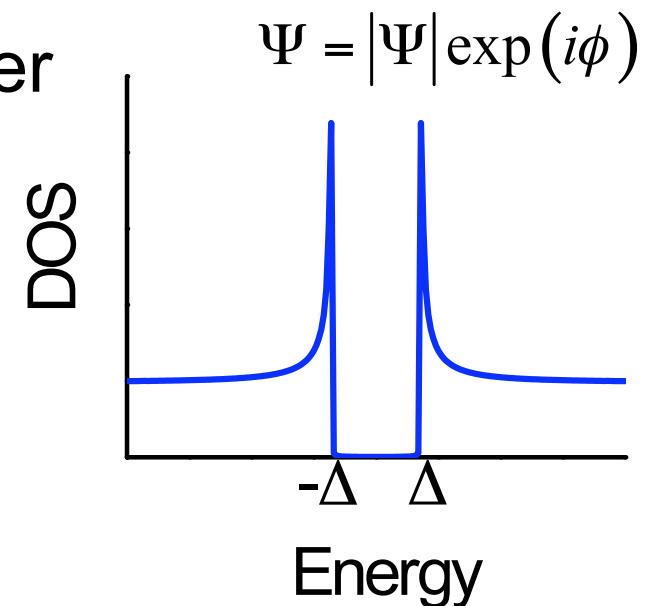
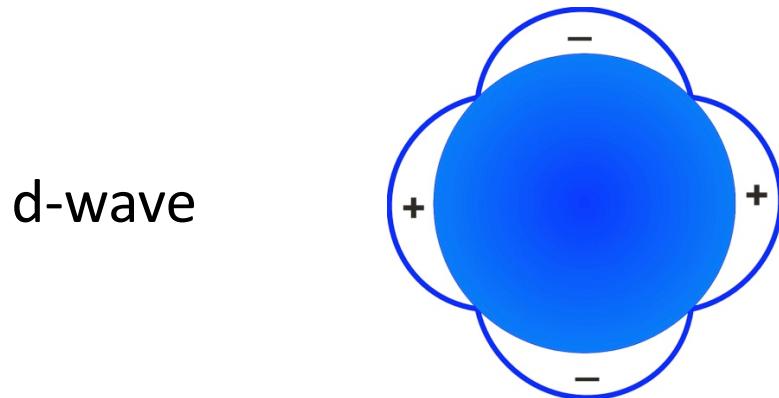
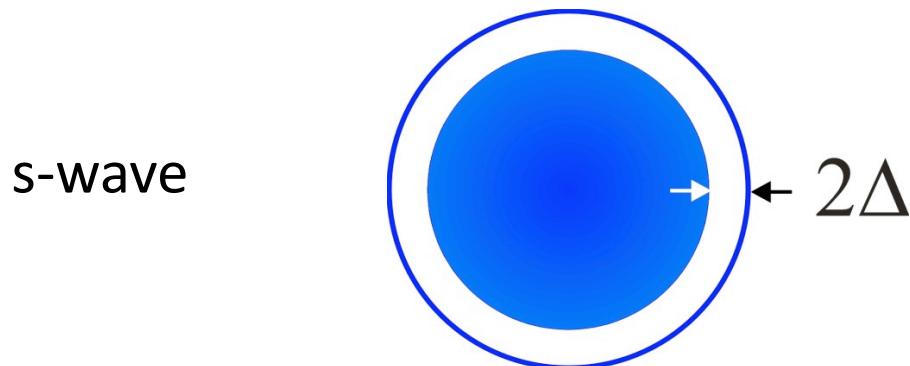


The central peak arises from Andreev Bound States, from broken reflection symmetry of the superconducting order parameter

Review: *d-wave SC and Andreev reflection ...*

Electron Tunneling Spectroscopy (VII)

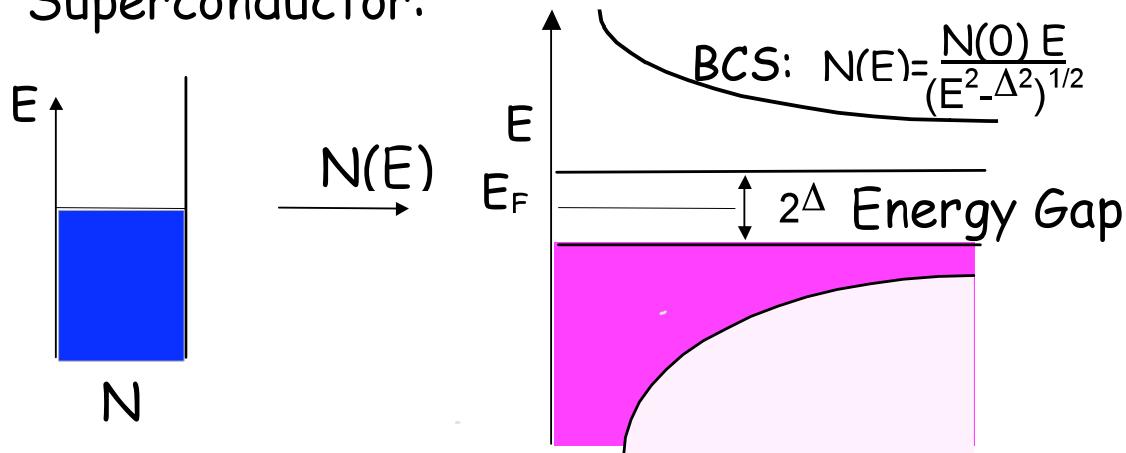
Superconducting Order Parameter



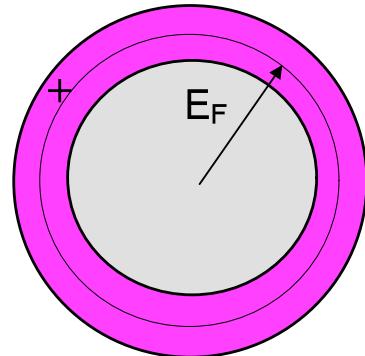
Electron Tunneling Spectroscopy (VIII)

(Gap / OP symmetry)

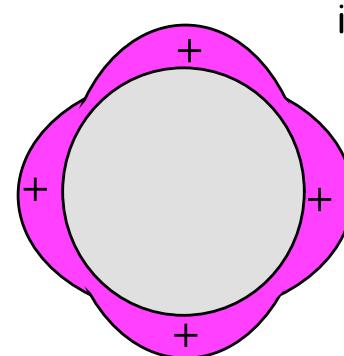
Superconductor:



Some possible symmetries:



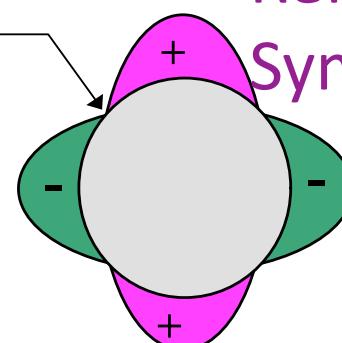
s-wave



anisotropic s-wave

“Conventional”

nodes
in gap



d-wave

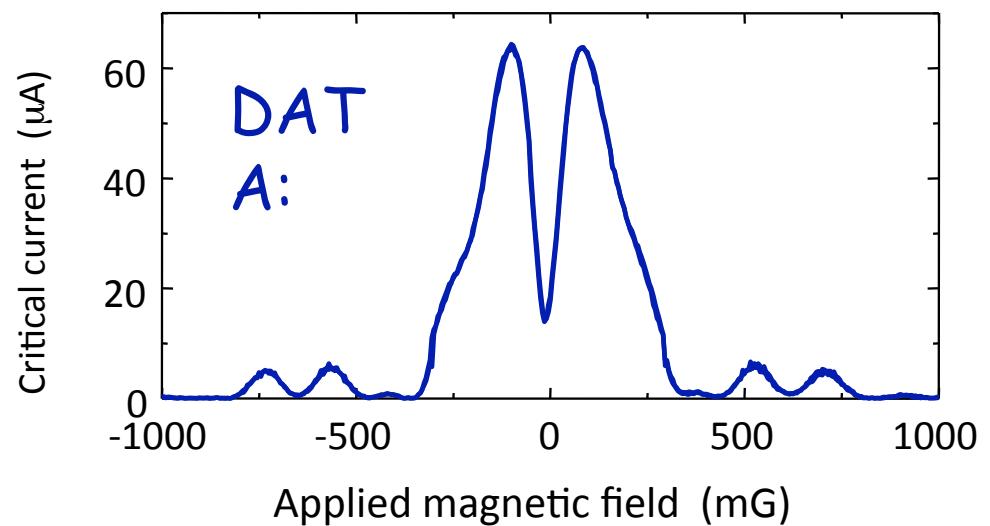
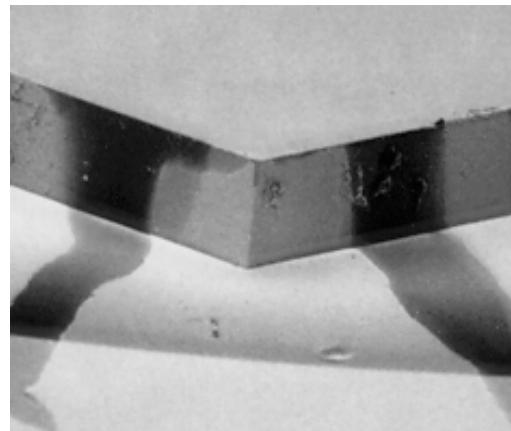
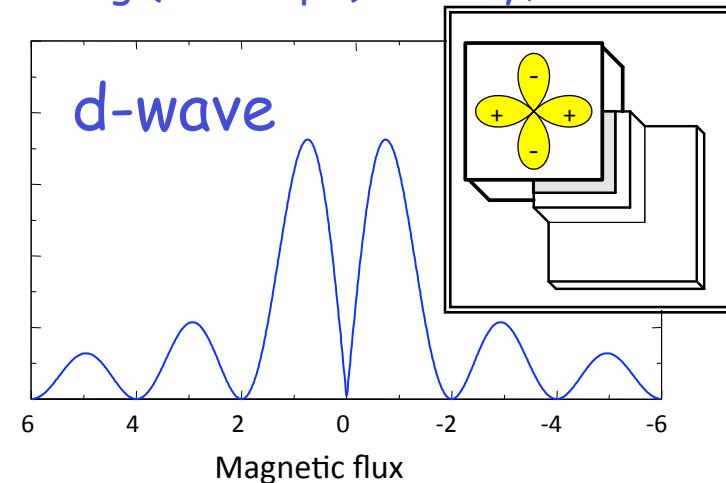
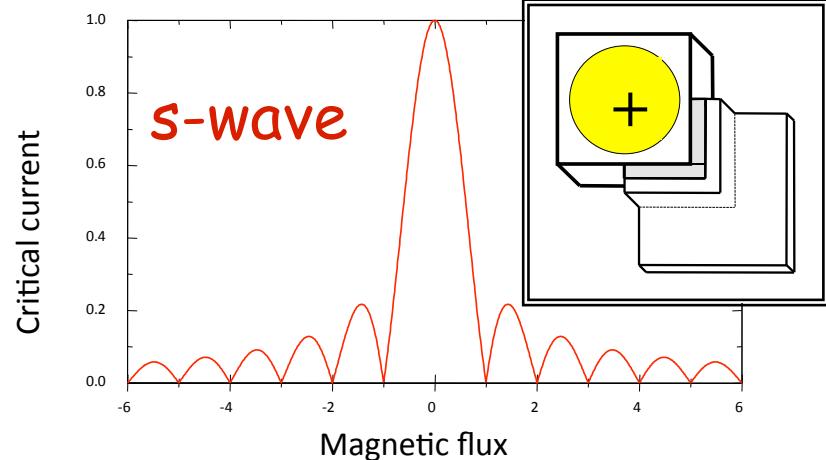
“Unconventional”

Broken
Reflection
Symmetry

D-wave was already shown:

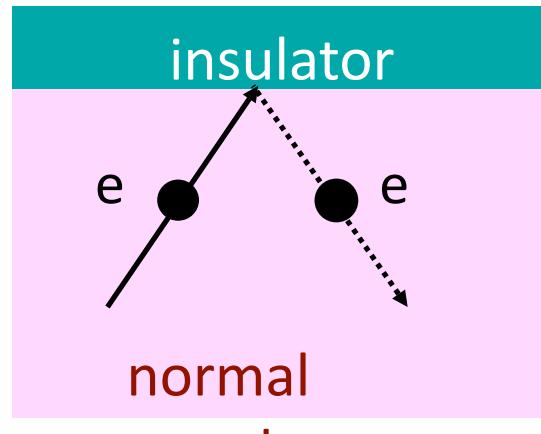
Josephson Junction (Wollman et al.)

1997 Buckley Prize: Van Harlingen, Ginsberg (this exp't); Kirtley, Tsui



Andreev Reflection (I)

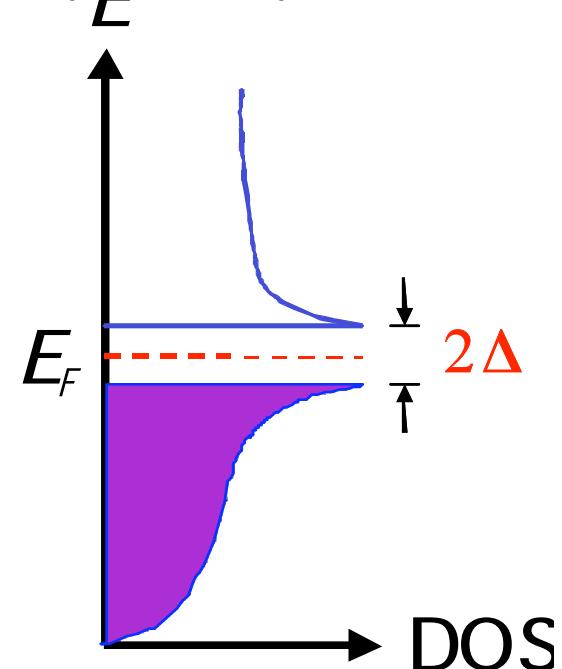
What will happen to an electron with $E < \Delta$ and no tunnel barrier?



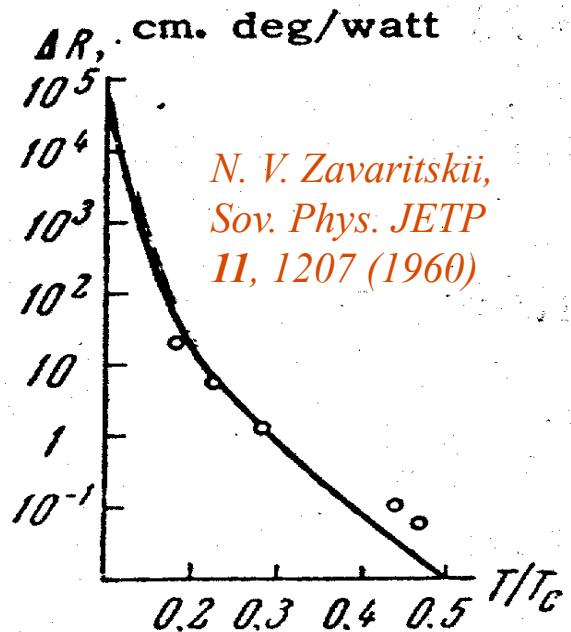
metal
specular reflection

- Within the gap, no quasiparticle states available, no single particles can enter S.
- Will a normal-metal/superconductor (N/S) system be less conductive than a single N?
 - No!

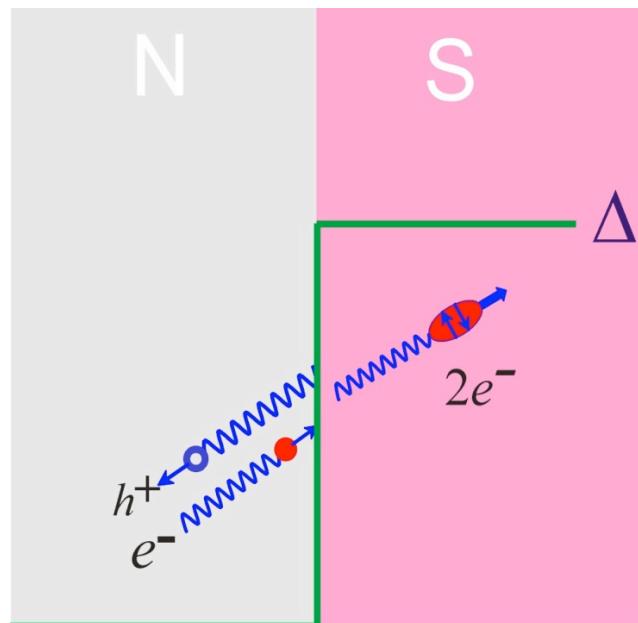
cf. At an interface with huge potential barrier that is translationally invariant along the transverse direction, incoming electrons reflect specularly.



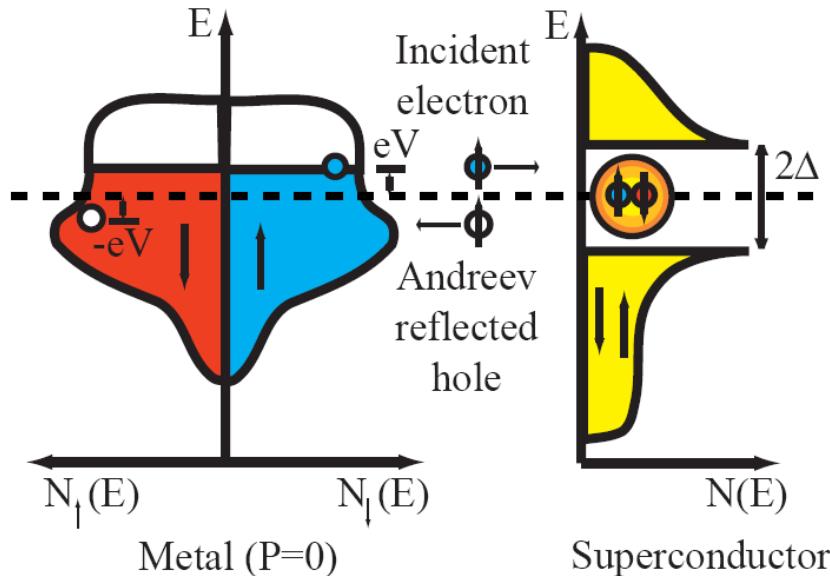
Andreev Reflection (II)



- QM scattering off SC pair potential near N/S
- Particle-hole conversion process multi-particle (AR) vs. single particle (tunneling)
- Retro-reflection $\mathbf{v}_h = -\mathbf{v}_e$

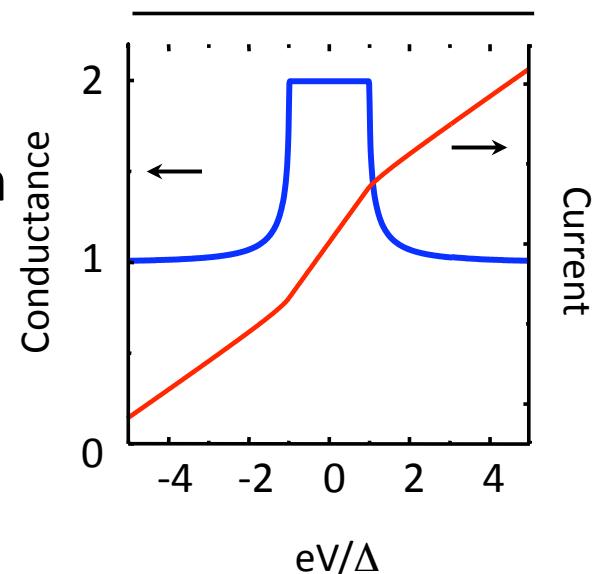


Andreev Reflection (III)



- Sub-gap conductance is doubled.
- Andreev reflected hole carries information on the phase of electron state and macroscopic phase of SC. phase change = $\Phi + \arccos(\epsilon/\Delta)$
- Inverse process ($S \Rightarrow N$): AR of a hole or
 - emission of a Cooper pair ("Andreev pairs"): **proximity effect**

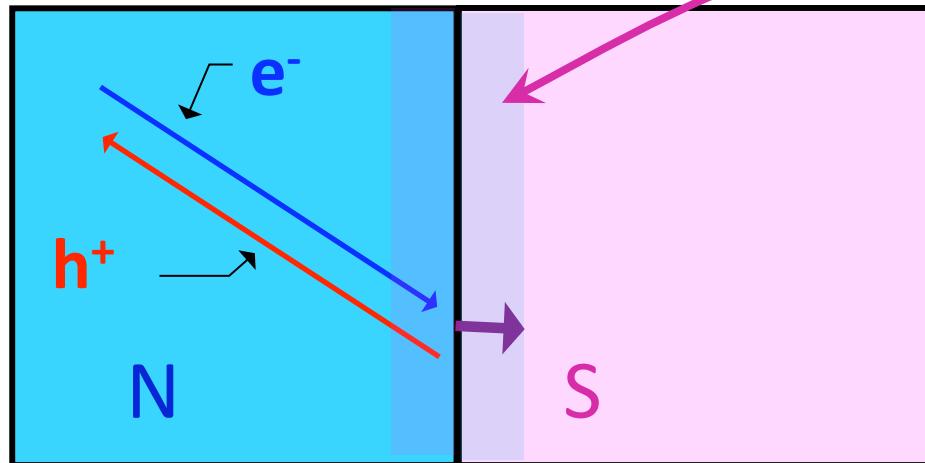
- Conserved quantities
 - Energy (E)
 - Momentum ($\hbar k$) ($\Delta \ll E_F$)
 - Spin (S)
 - Charge inc. Cooper pairs



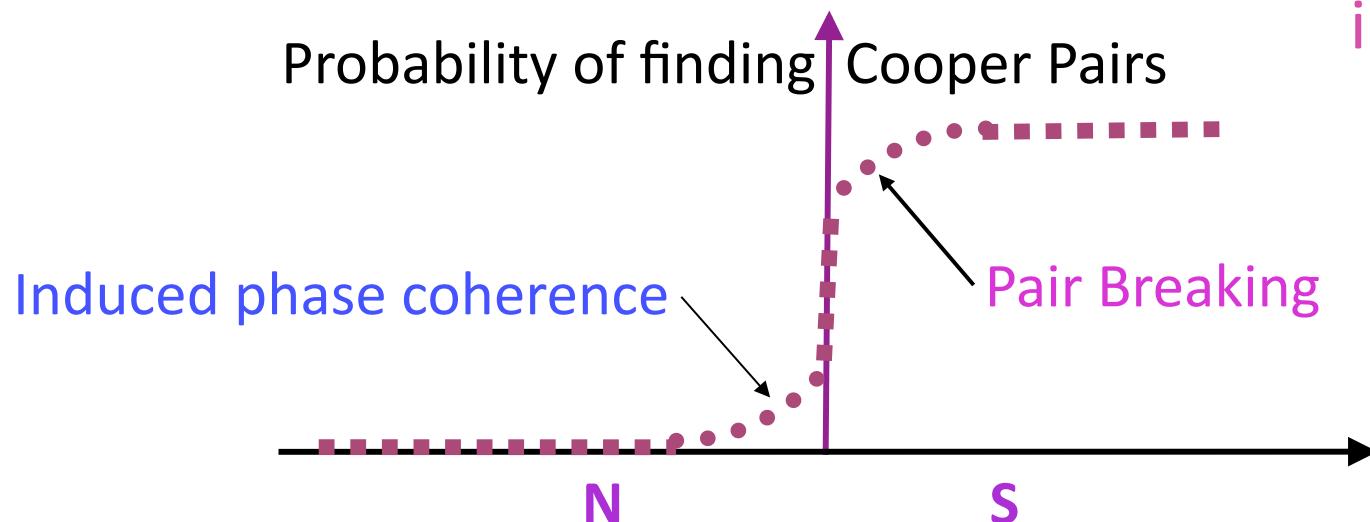
Andreev Reflection (IV) (definition)

Normal Metal/Superconductor (N/S) interface

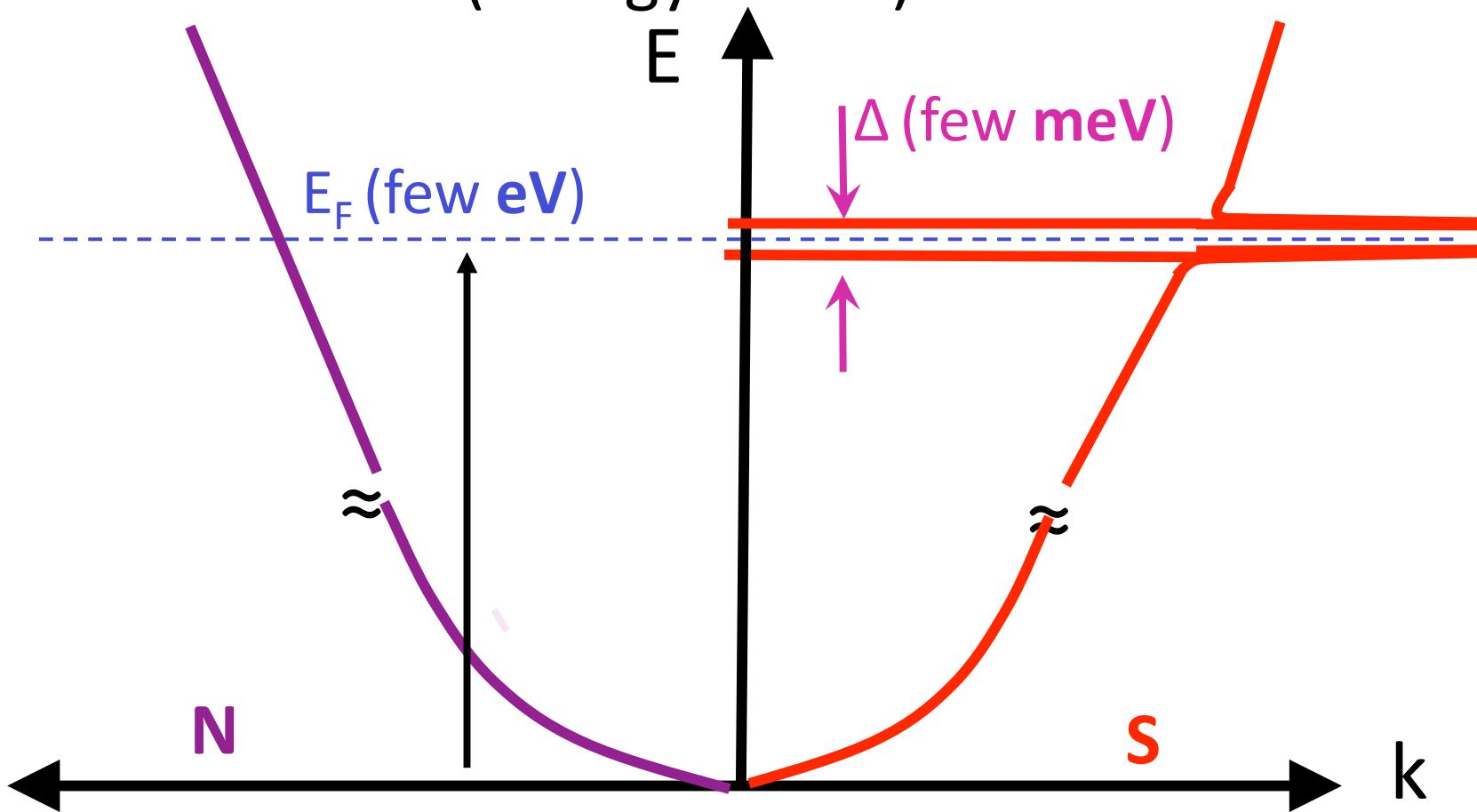
In N:
Electrons
retro-
reflected as
holes



In S:
Cooper
Pairs
Broken
near
interface



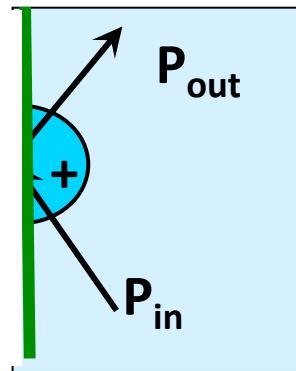
Andreev Reflection (V) (energy scales)



Particle conversion process that conserves
charge, energy and momentum!

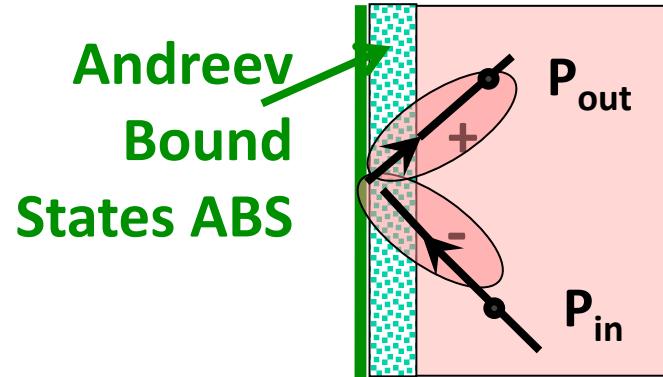
Andreev Reflection (VI)

(within a superconductor)



s-wave:

No Andreev Reflection
(order parameter isotropic)
⇒ Cooper Pairs
not Broken



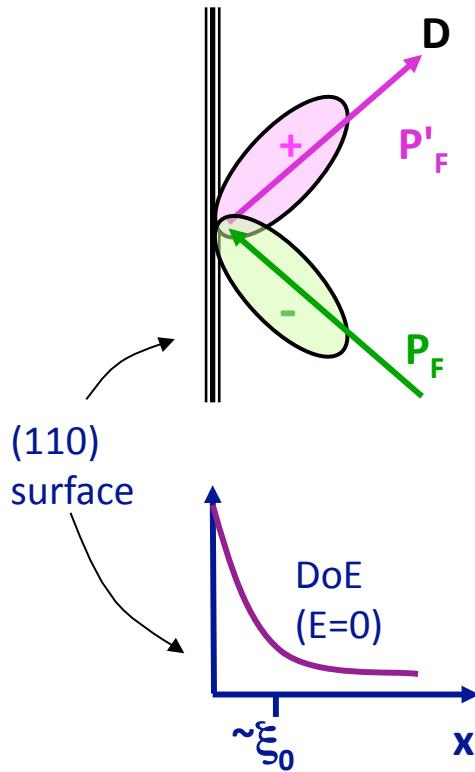
d-wave:

Strong Andreev Reflection
(order parameter sign change)
⇒ Cooper Pairs
Broken

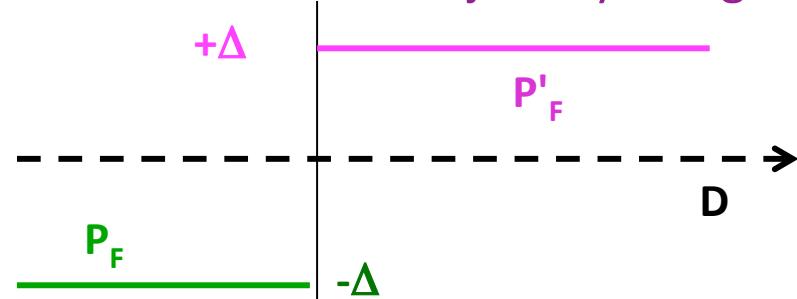
Quasiparticles nucleate at surface forming
Andreev Bound States
(Bound w/in ~coherence length of surface)

Andreev Reflection (VII)

(Andreev bound states, ABS)

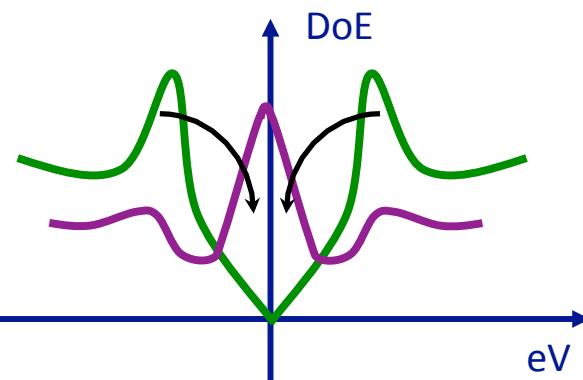


Cooper Pair Quasi-Classical Trajectory along D :



Sign-change of OP is only Boundary Condition in the Solution to Andreev Equations: Quasiparticle Bound States at surface (decay $\sim \xi_0$)

Peak at zero bias (Fermi energy) arises from quasiparticles at Fermi energy in near-surface region



Electron Tunneling Spectroscopy (IX)

(Diagnostics of ZBCP - a)

Several phenomena will produce a ZBCP
(zero-bias conductance peak) in tunneling

1. Magnetic scattering (spin-flip, Kondo)
2. Proximity effects
3. Josephson current
4. Shorts / pinholes through tunnel barrier
5. Cooper-pair tunneling
6. Reflectionless tunneling
7. Inelastic processes
8. ABS (Andreev bound states)
.....etc., etc.,.....

DIAGNOSTICS are REQUIRED to determine
if the zero bias conductance peak arises from ABS
(intrinsic to any unconventional superconductor)

Electron Tunneling Spectroscopy (X)

(Diagnostics of ZBCP - b)

1. Crystallographic orientation

- Only seen in ab-plane tunneling (not in c-axis)
- Not seen in specular (100) a-axis tunneling
- Magnitude depends upon ab-plane crystallographic orientation

2. Temperature

- Split in ZBCP below T_s
- Zero-bias conductance $\sim 1/T$ below 40K, above T_s

3. Magnetic Field

- Field Evolution
- Saturation effects
- Field Scale
- Angular or orientational dependence of the applied field
- Hysteresis

4. Doping and disorder

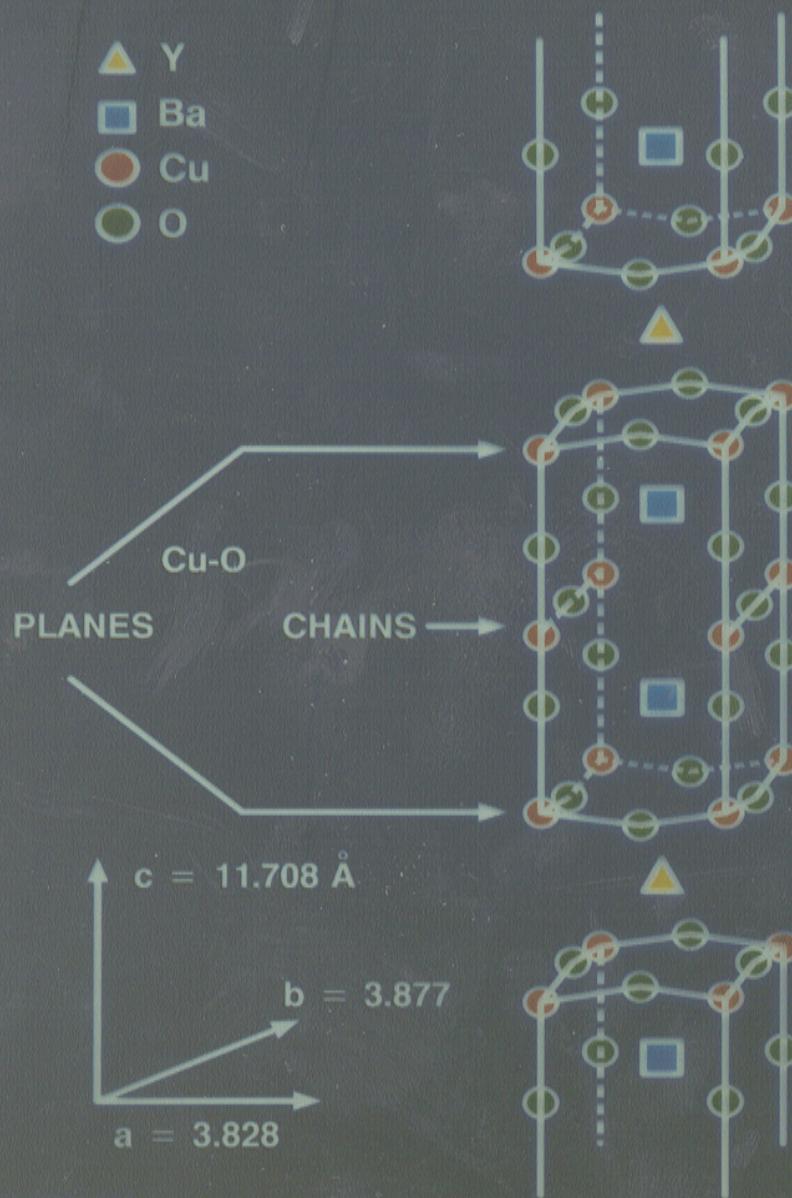
- ZBCP reduces in size and disappears with increased doping and ion-induced damage.
- This is shown to be a DoS effect (follows gap disorder dependence)

∴ Observed Zero Bias Conductance Peaks arise from ABS

CRYSTAL STRUCTURE



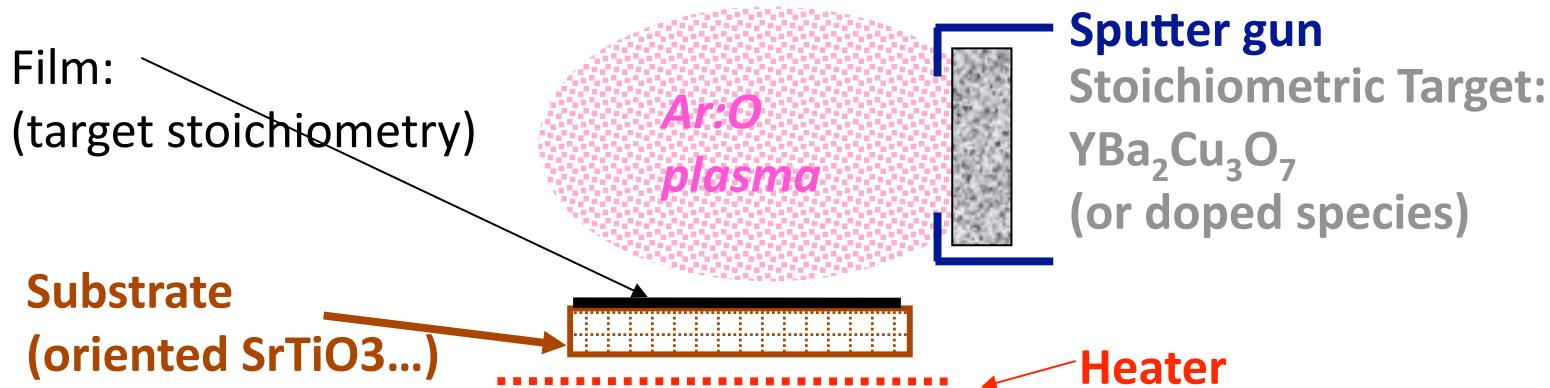
- ▲ Y
- Ba
- Cu
- O



Electron Tunneling Spectroscopy (XI)

(Film growth and diagnostics)

Off-Axis Planar Magnetron Sputter Deposition:



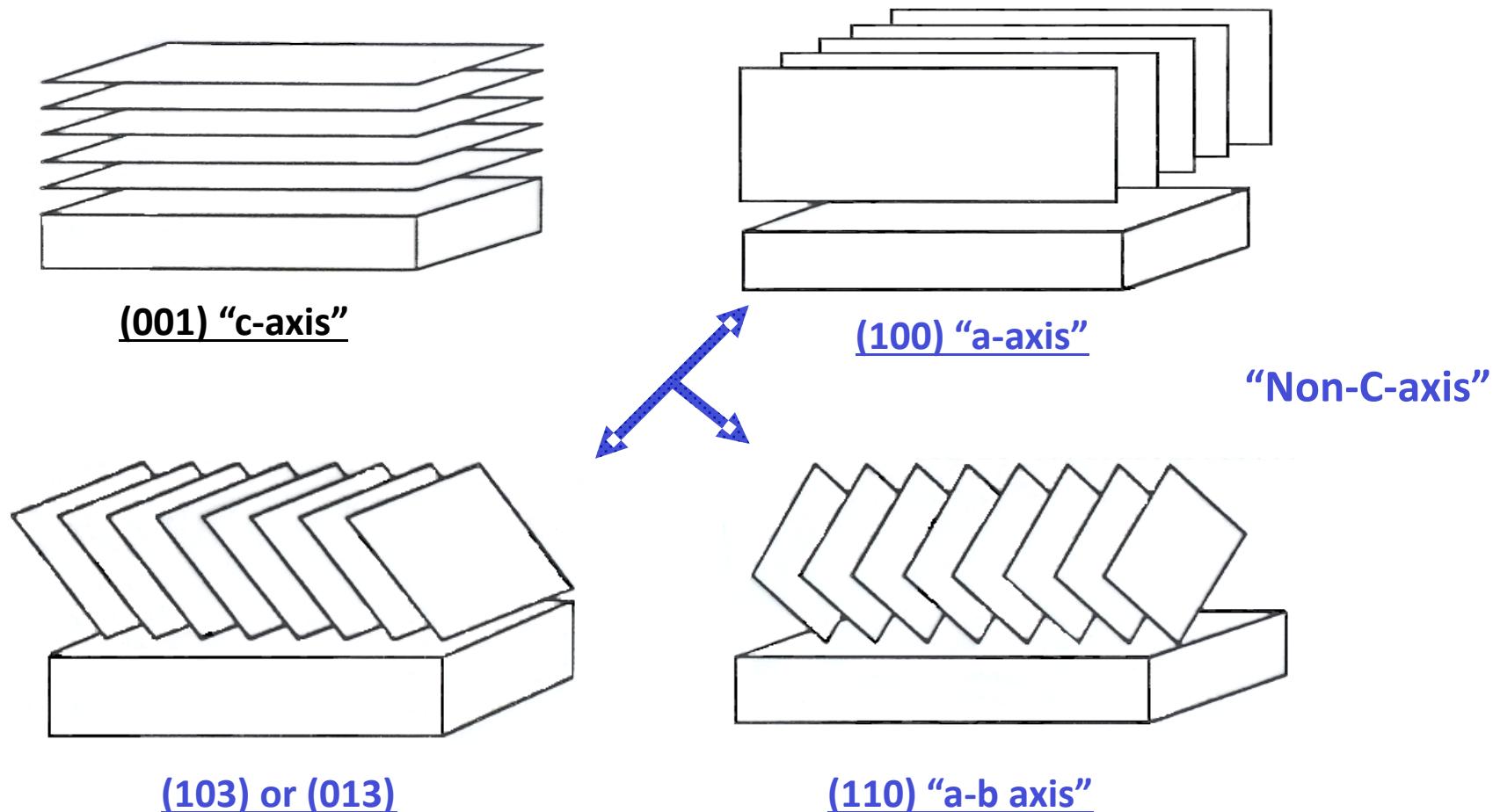
Reproducible films of (001), (100) and (103) and (110)-oriented $\text{YBa}_2\text{Cu}_3\text{O}_7$,
 $(\text{Y}_{x}\text{Pr}_{1-x})\text{Ba}_2\text{Cu}_3\text{O}_7$, $\text{YBa}_2(\text{Cu}_x\text{Ni}_{1-x})_3\text{O}_7$, $\text{YBa}_2(\text{Cu}_x\text{Zn}_{1-x})_3\text{O}_7$

Materials Analysis includes:

- Electronic transport (resistivity vs. temperature, tunneling)
- Magnetization (susceptibility vs. temperature)
- Structural analysis (XRD, RBS, SEM, AFM, etc.,...).

Electron Tunneling Spectroscopy (XII)

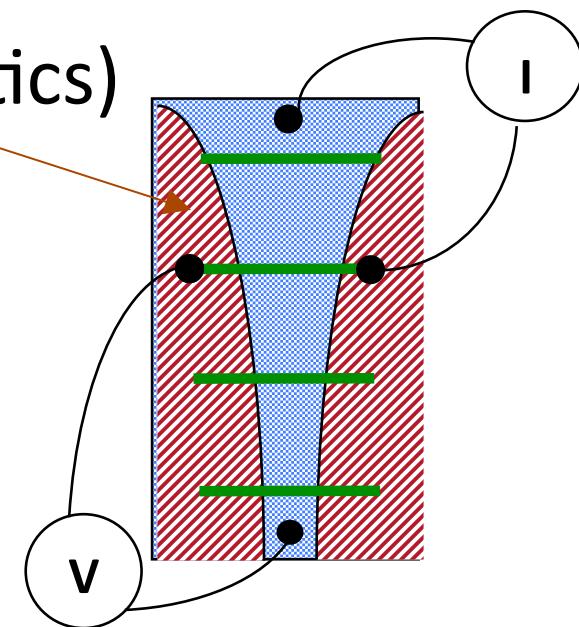
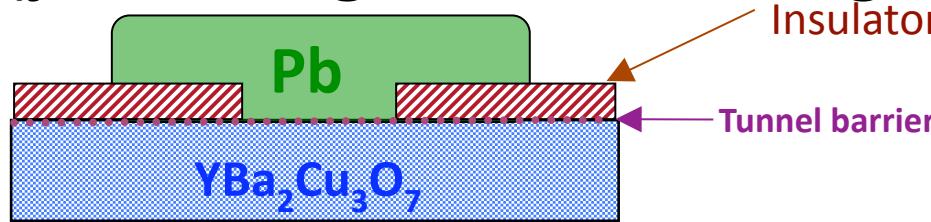
Possible Orientations of CuO₂ Planes



YBCO thin films, or cut crystal faces

Electron Tunneling Spectroscopy (XIII)

(junction growth and diagnostics)



- Pb counter-electrodes evaporated *ex-situ*.

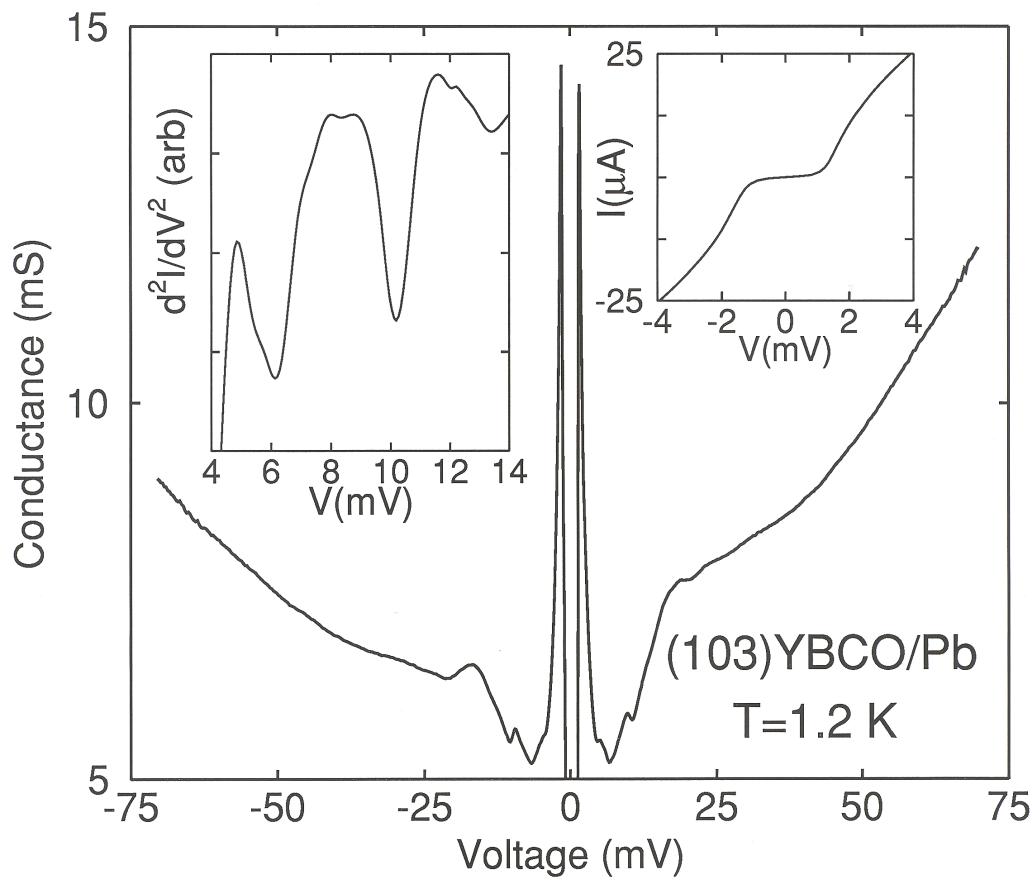
TUNNELING VERIFIED by:

1. Quality of the observed Density of States (DoS) of the superconducting Pb counter electrode, OR the now well-known YBCO DoS
2. Junction resistance: scales with $1/A_{\text{junction}}$
3. Little to no temperature dependence
4. **REPRODUCIBILITY**

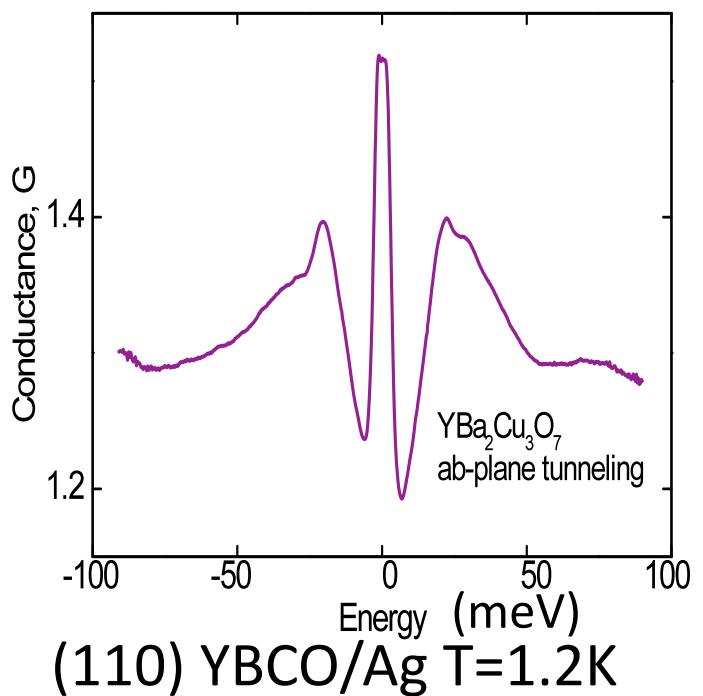
Electron Tunneling Spectroscopy (XIV)

(Junction diagnostics: DoS)

Many ways to grow REPRODUCIBLE junctions for planar tunneling spectroscopy

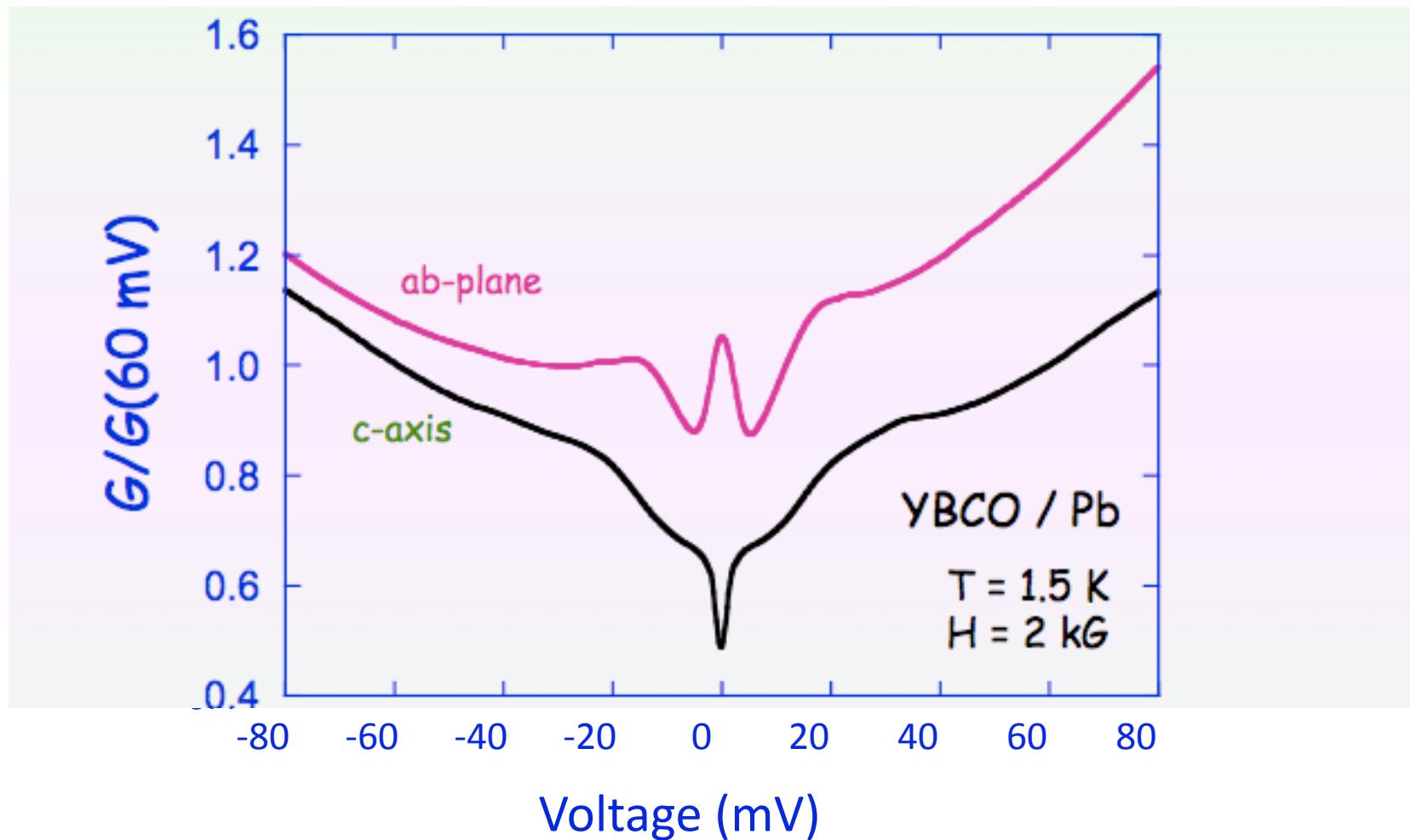


+V → filling YBCO states



Electron Tunneling Spectroscopy (XV)

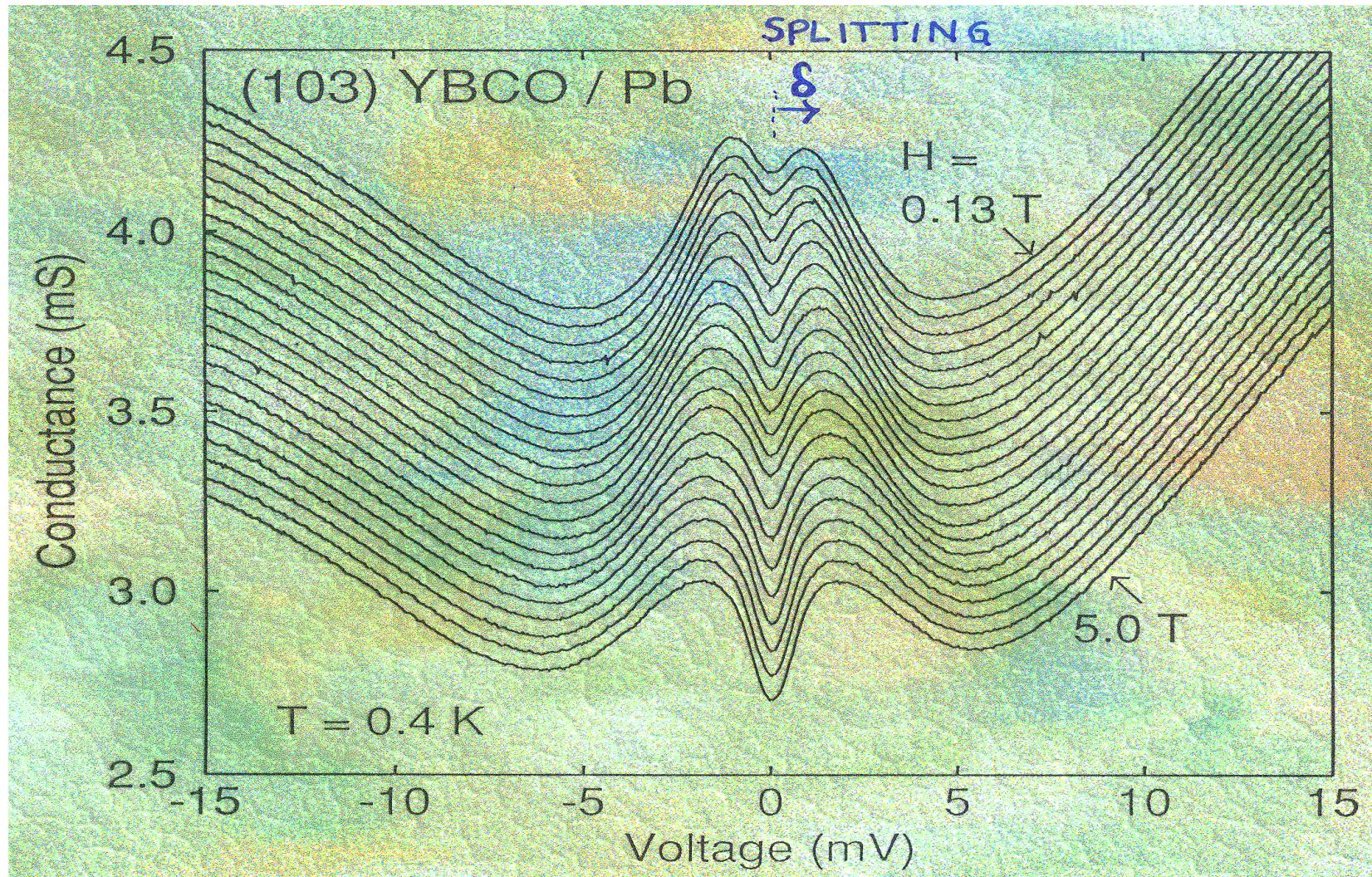
(Junction diagnostics: Crystallographic Orientation



M. Covington & LHG, PRB **62**, 12440 (2000)

Electron Tunneling Spectroscopy (XVI)

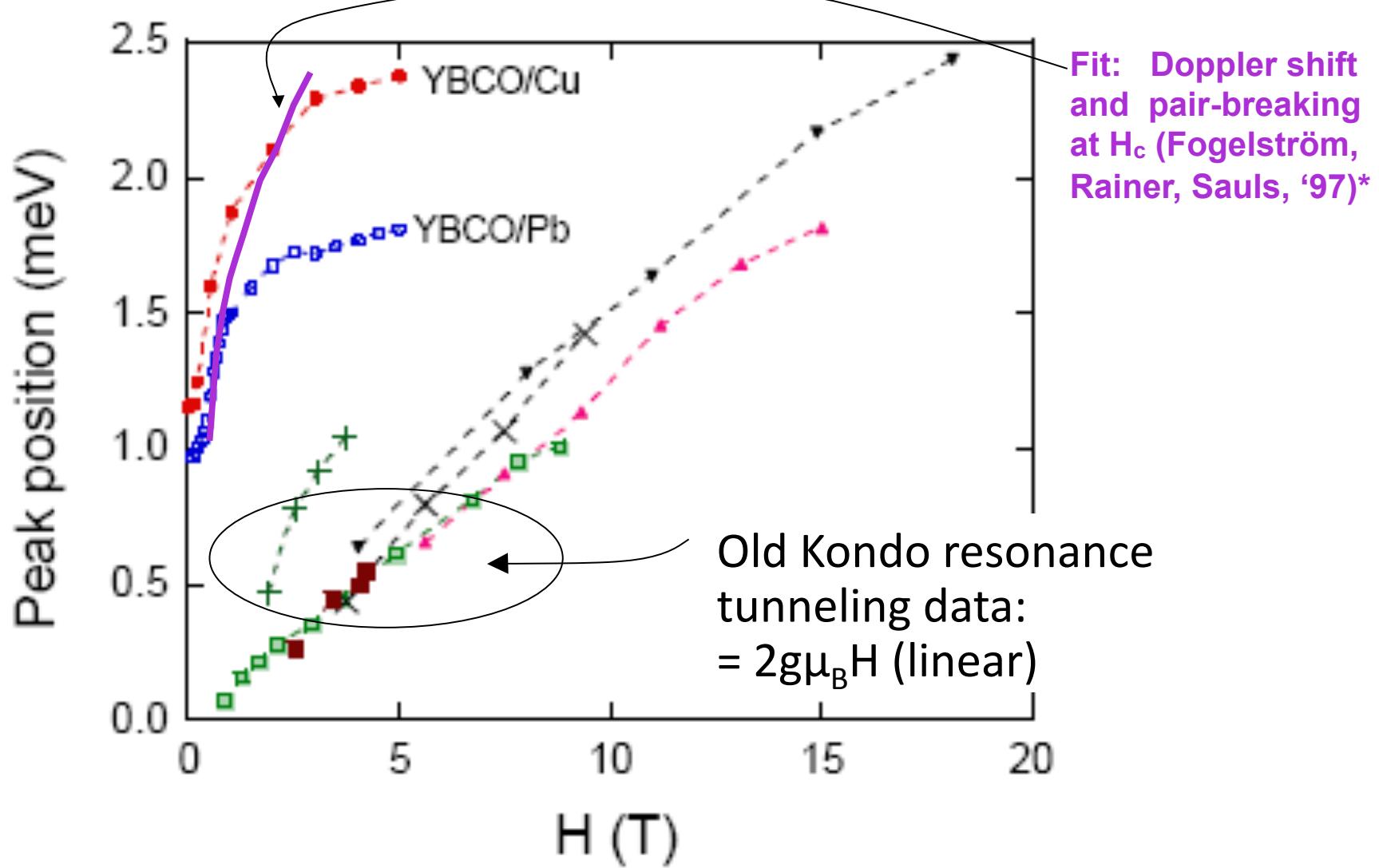
(Magnetic field dependence - a)



J. Lesueur et al, Physics C (1992); M. Covington et al, PRB (2000)

Electron Tunneling Spectroscopy (XVII)

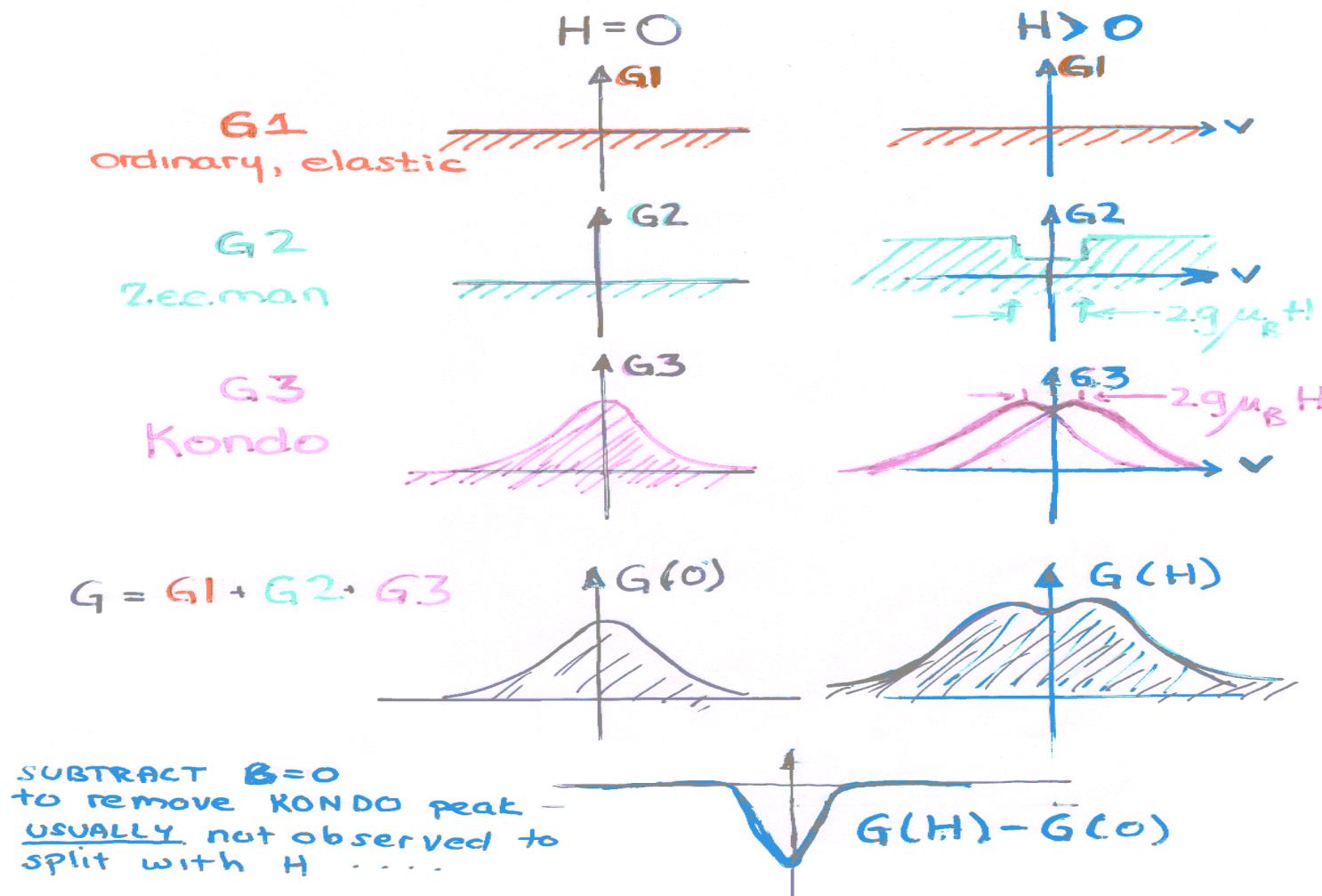
(Magnetic field dependence - b)



*Lesueur, (92-00); Covington (97-00); Aprili (99); Deutscher (99-05)....

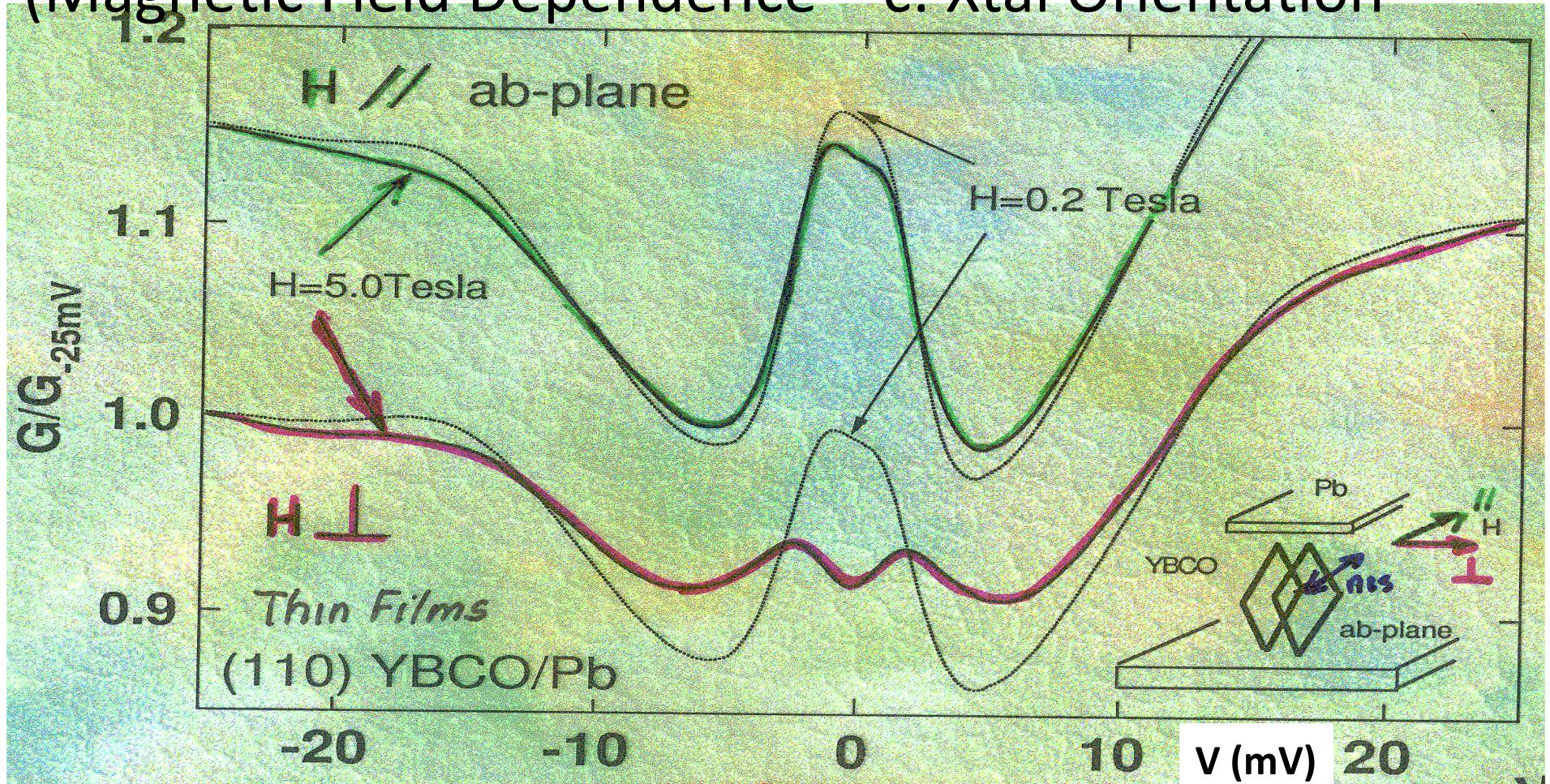
Electron Tunneling Spectroscopy (XVIII)

Anderson - Applebaum Model:



Electron Tunneling Spectroscopy (XIX)

(Magnetic Field Dependence – c: Xtal Orientation



Highly - anisotropic QP transport: ABS carry current parallel ab-planes (*not in c-axis direction*)! Splitting $\propto V_F \cdot P_s$

M. Aprili et al, PRL (1999); Krupke et al PRL (1999)

Electron Tunneling Spectroscopy (XX)

(Origin of field splitting)
Andreev bound states carry current along the interface

Applied Magnetic field, H_{appl} , induces a Doppler Shift:

$$\delta = \delta_s + (e/c) v_F \lambda \sin\phi_c H_{appl}$$

δ = ABS splitting

λ = penetration depth

splitting $\propto H_{applied}$

v_F = of tunneling electrons

ϕ_c = tunneling cone

Magnetic fields intrinsically break time reversal symmetry,
Here, field-driven BTRS is detected by a splitting of ZBCP.

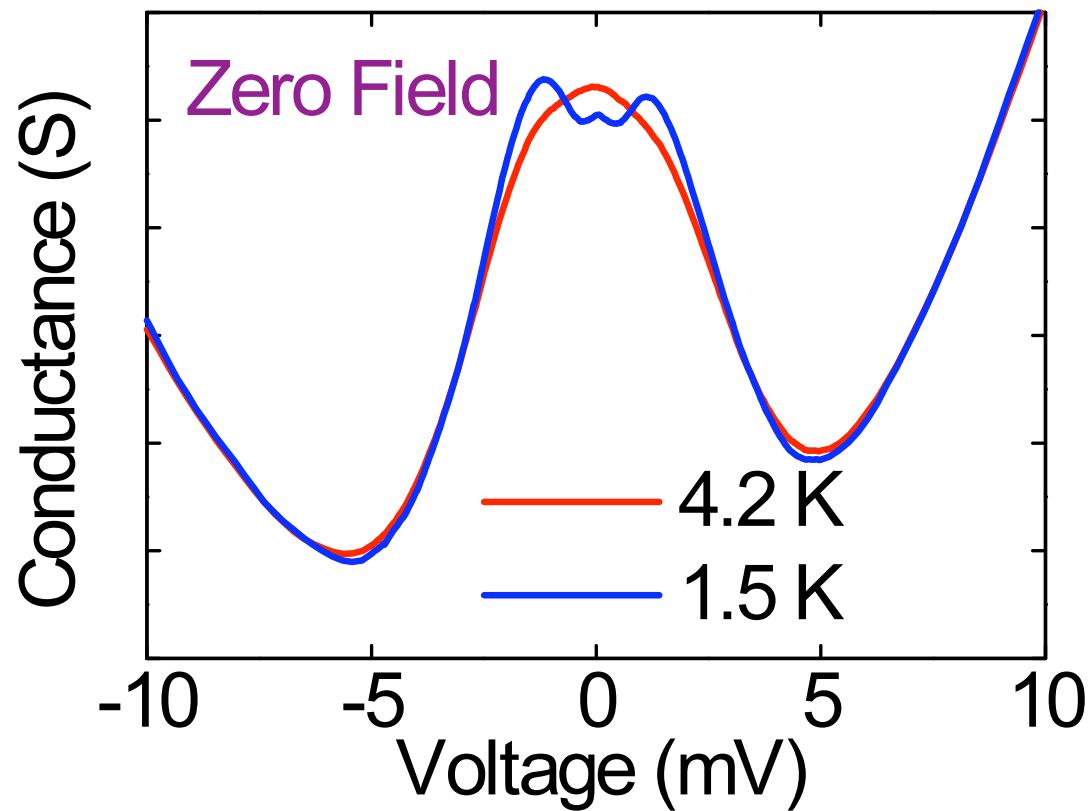
∴ Splitting of the ABS in ZERO field ⇒
SPONTANEOUSLY Broken Time-Reversal Symmetry

Electron Tunneling Spectroscopy (XXI)

(Zero-field splitting)

Consistent with

- ⇒ Spontaneous Surface Currents
- ⇒ Spontaneously Broken Time Reversal Symmetry



Electron Tunneling Spectroscopy (XXII)

(BTRS – a: Phase diagram)

Mechanism (Laughlin; Matsumoto & Shiba) and
Phase Diagram (Fogelström, Rainer, and Sauls

- QUASIPARTICLES form near surface (Andreev bound state)

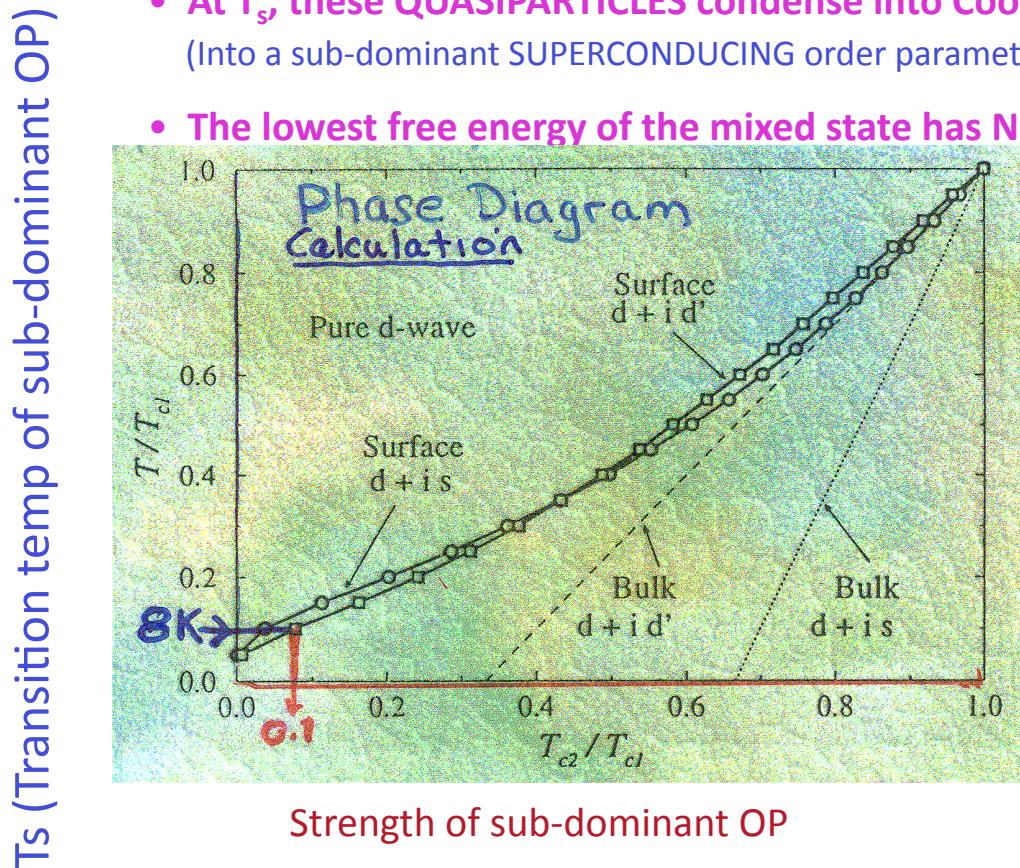
(Due to the reflection symmetry breaking of d-wave)

- At T_s , these QUASIPARTICLES condense into Cooper pairs

(Into a sub-dominant SUPERCONDUCTING order parameter: s-wave likely)

- The lowest free energy of the mixed state has NO NODES

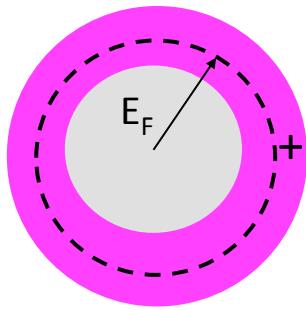
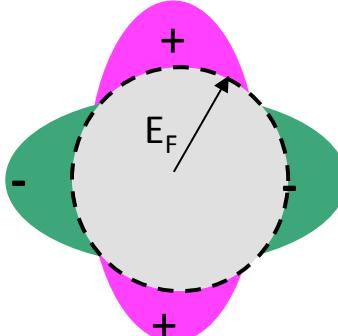
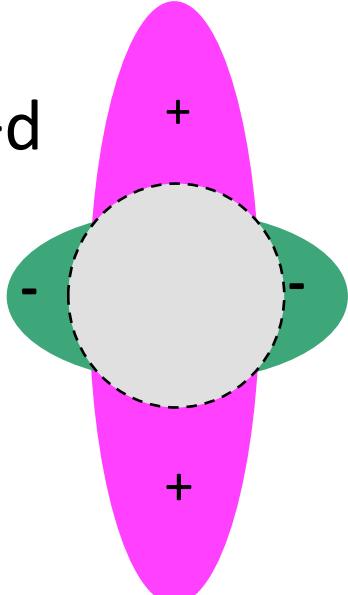
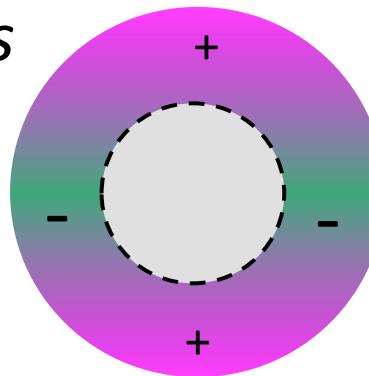
$\rightarrow d+is ?$



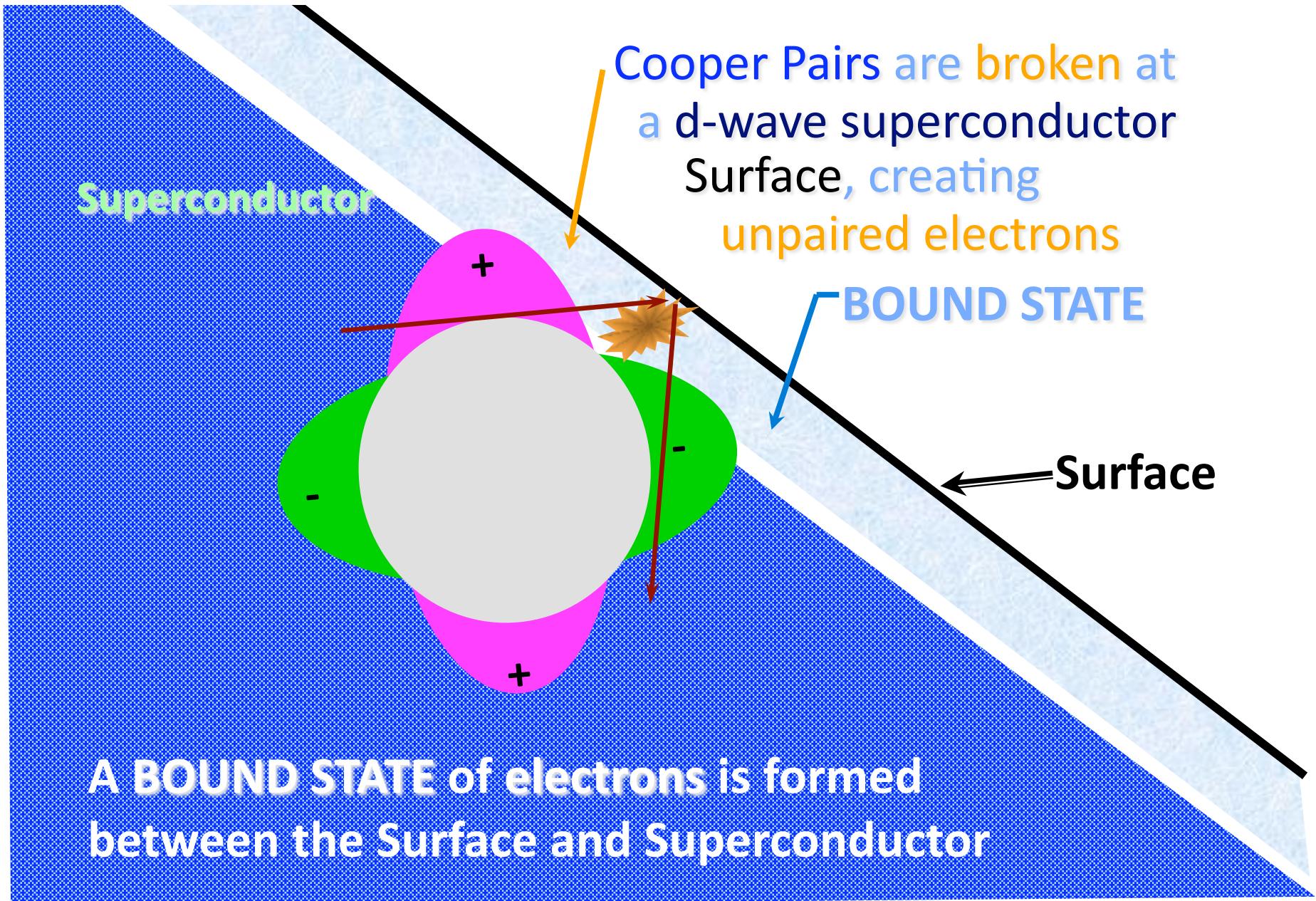
We measure $T_s = 8.1\text{K}$
At T_s , phase diagram
predicts splitting,
 $\delta=1.05 \text{ meV}$
We measure $\delta=1.16 \text{ meV}$

Electron Tunneling Spectroscopy (XXIII)

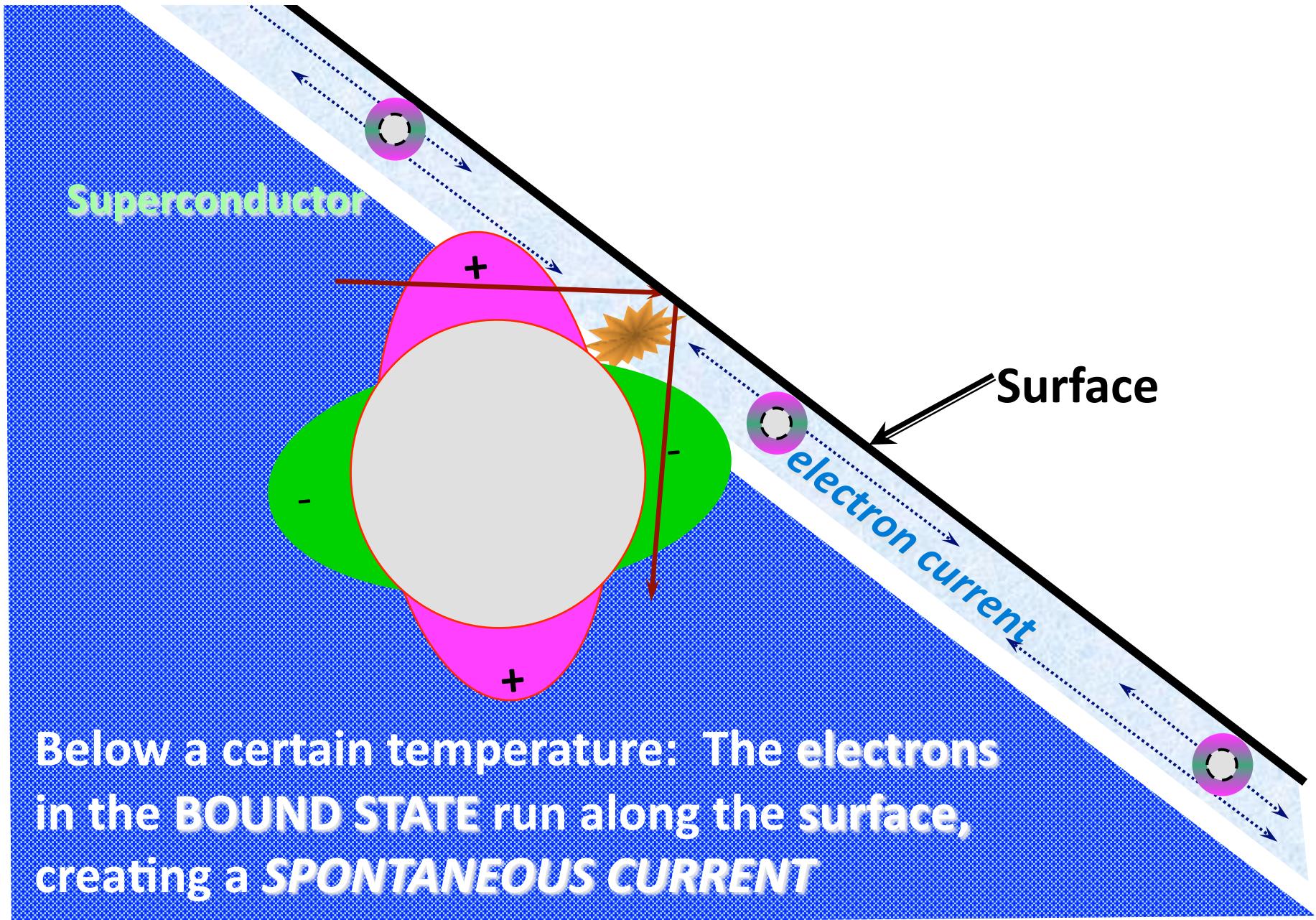
(BTRS –b: Mixed States)

- s 
 - d 
 - $s+d$ 
 - $d+is$ 
- Breaks Time-Reversal Symmetry*

(Cartoon of ABS: $T < T_c$; $T > T_s$)



(Cartoon of BTRS $T < T_s$ ($\sim 8K$))



Conclusions

Careful control/growth of materials, systematic diagnostics and reproducibility are crucial in the study of the physics of novel materials

High-T_c Superconductors Spontaneously
Break Three Symmetries:

Gauge	(superconducting)
Reflection	(d-wave)
Time-Reversal	(spontaneous magnetic fields)

Planar Tunneling is Powerful Phase-Sensitive Probe of
Unconventional Superconductivity

Cast of Characters (best part)

Wan Kyu Park

Patrick Hentges (Intel, OR)

Herve Aubin (ESPCI, Paris)

Marco Aprili (ESPCI, Orsay)

Jerome Lesueur (ESPCI, Paris)

Elvira Badica (U. VA)

Mark Covington (Seagate)

Margaret Pafford (Rohm & Hass)

Glenn Westwood

Walter G. Klemperer

Chad Mirkin

Sha Jian

David G. Hinks

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Chemistry UIUC

Chemistry NWU

MatSci ANL

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