Freiberg University of Mining and Technology, Germany



## Thermodynamics of High Temperature Materials Systems

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#### **Thermodynamics of High Temperature Materials Systems**

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## **Outline**

#### **1. Introduction and motivation for thermodynamic calculations**

- Computational thermodynamics
- CALPHAD approach (CALculation of PHAse Diagrams)
- Thermodynamic databases and software
- 2. Thermodynamic optimization of the Ce-O system
  - Thermodynamic modeling of solution phases
- 3. Precursor-derived Si-(B-)C-N ceramics
  - High temperature reactions of silicon carbide and silicon nitride ceramics
  - Crystallization and high temperature stability of Si-(B-)C-N ceramics

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## **Outline**

- 4. Computational thermodynamics in heat shield engineering
  - The Y-Si-C-O system database
  - Active / passive oxidation of SiC
  - Phase reactions of Yttrium silicates and C/C-SiC composites
  - High temperature stability issues in the engineering of heat shields
- **5.** Conclusions

## **Combined Approach**





CALPHAD

**CALculation** of PHAse Diagrams

### **CALPHAD** (CALculation of PHAse Diagrams)

- Development of Optimized Thermodynamic Datasets stored in Computer Databases
- **Calculation of :** 
  - Thermodynamic Functions
  - Liquidus Surface
  - Isothermal Sections
  - Isopleths
  - Potential Phase Diagrams

- Phase Fraction Diagrams
- Phase Compositions
- Scheil Solidification

**Requires Modeling of Stoichiometric and Solution Phases Taking into Account the (Crystal-) Structures and Site Occupancies** 

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## CALPHAD (CALculation of PHAse Diagrams) Software

- LUKAS (BINGSS, BINFKT, TERGSS, TERFKT)
- THERMO-CALC
- FACTSAGE
- PANDAT
- MALT, MALT2
- MTDATA
- JMATPRO
- GEMINI
- •••

### CALPHAD (CALculation of PHAse Diagrams) Databases

- SGTE, Scientific Group Thermodata Europe
  - SSOL2, SSOL4
  - SSUB3
  - Noble Metals
- Thermo-Calc: Steels, Ni-base, slags, ...
- ThermoTech: Ni-base, Al-, Mg-, ...
- PML: Al-, Ceramics

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# Calculated Ce–O System in Solid State from 60 to 67 mol. % O in comparison with experimental data.



Phases in the Partial Ce – O System

**Related Crystal Structures:** 

**CeO<sub>2-x</sub> (ss)** CaF<sub>2</sub> - type (Strukturbericht C1)

Compound Energy Formalism:  $(Ce^{+3}, Ce^{+4})_1(O^{-2}, Va)_2$ 



**C-Ce<sub>2</sub>O<sub>3</sub> (ss)** Mn<sub>2</sub>O<sub>3</sub> - type (Strukturbericht D5<sub>3</sub>, Ordered State of C1) Unit Cell: composed of 8 CaF<sub>2</sub>-type cells. ¼ of O-ions removed, remaining atoms re-arrange towards these vacancies. Compound Energy Formalism:  $(Ce^{+3}, Ce^{+4})_2(O^{-2})_3(O^{-2}, Va)_1$ 

Contains more O atoms than the ideal formula of the  $Mn_2O_3$ .

**Ce<sub>2</sub>O<sub>3</sub>** Stoichiometric phase description (Strukturbericht D5<sub>2</sub>)

"Compound Energy" Formalisms – Reference Compounds

## (A,B)<sub>k</sub>(D,E)<sub>I</sub> Solution phase with two sublattices and 4 species

Four compounds defined:

A : D A : E B : D B : E

Gibbs free energy for every compound to be determined

Here:  $(Ce^{+3}, Ce^{+4})_1(O^{-2}, Va)_2$ 





(A,B)<sub>k</sub>(D,E)<sub>l</sub> Solution phase with two sublattices and 4 species

Modeling of solution phases; sublattice model described in the Compound Energy Formalism

(A,B)<sub>k</sub>(D,E)<sub>I</sub> Solution phase with two sublattices and 4 species

$$-S_{\rm m}^{\rm mix}T = RT \sum n^{\rm s}y_{\rm J}^{\rm s}\ln(y_{\rm J}^{\rm s})$$

- $n^{s}$  Stochiometric coefficient (s: sublattice)
- $y_{A}^{s}$  Site fraction of spezies A on sublattice s

 $\Sigma v_{\rm I}^{\rm s} = 1$ 

**Compound Energy Formalism – Excess term of Gibbs free energy** 

(A,B)<sub>k</sub>(D,E)<sub>I</sub> Solution phase with two sublattices and 4 species

$${}^{\mathrm{E}}G_{\mathrm{m}} = \Pi y_{\mathrm{J}}^{\mathrm{s}} \sum y_{\mathrm{B}}^{\mathrm{t}} L_{\mathrm{A,B:D:G}} + \Pi y_{\mathrm{J}}^{\mathrm{s}} \sum y_{\mathrm{B}}^{\mathrm{t}} y_{\mathrm{D}}^{\mathrm{u}} L_{\mathrm{A,B:D,E:G}} + \dots$$

**Compound Energy Formalisms – Gibbs free energy of solution phases** 

$$\begin{aligned} \textbf{Mixing Gibbs Energy} &= \sum \Delta_{f}^{\circ} G_{end} \Pi y_{J}^{s} \\ &+ RT \sum \sum n^{s} y_{J}^{s} \ln(y_{J}^{s}) + {}^{E} G_{m}. \end{aligned}$$

#### **Phases in the Partial Ce – O System**

**CeO<sub>2-x</sub> (ss)** CaF<sub>2</sub> - type (Strukturbericht C1)

Compound Energy Formalism:  $(Ce^{+3}, Ce^{+4})_1(O^{-2}, Va)_2$ 



Cubic close pack of Ce ions, where all the tetrahedral voids form the sublattice on which the 2-x O-ions are statistically distributed. **Electroneutrality condition** determines that site fractions on the two sublattices are not independent: Single variable y is equal 2-x.

$$y'_{Ce^{+3}} = y$$
  $y''_{Va} = \frac{y}{4}$   
 $y'_{Ce^{+4}} = (1 - y)$   $y''_{O^{-2}} = \frac{1 - y}{4}$ 

No.	Paper	Experimental Technique	Measured Quantity	Composition	Temperature (K)	Remark
1.	Bevan & Kordis (1964)	Experiment with $CO_2/CO$ & $H_2O/H_2$	Partial pressures O <sub>2</sub>	CeO <sub>1.5-</sub> CeO <sub>2</sub>	909 - 1442	+
2.	Ackerman & Rauh (1971)	Mass Spectroscopy & Mass Effusion	Partial pressures CeO, CeO <sub>2,</sub> Ce(g), CeO	$\begin{array}{c} \text{CeO}_{1.51} - \\ \text{CeO}_{1.53} \\ \text{CeO}_{1.5} - \\ \text{CeO}_{1.34} \end{array}$	2000 - 3000 1600 - 2000 1825 - 2320 1550 - 2040	+
3.	Iwasaki & Katsura (1971)	Experiment with $CO_2 \& CO_2 / H_2$ mixture	Partial pressures O <sub>2</sub>	CeO <sub>2.00</sub>	900, 1000, 1100, 1227, 1300	+
4.	Campserveux & Gerdanian (1978)	Micro- Calorimetry	Partial pressures O <sub>2</sub>	CeO <sub>2</sub>	1353, 1296, 1244	+
5.	Kitayama et al. (1985)	Thermo- gravimetry	Partial pressures O <sub>2</sub>	$\begin{array}{c} CeO_2, \\ Ce_2O_3Ce_3O_5 \end{array}$	1000 – 1330	+

6.	Marushkin et al. (2000)	Knudsen cell, Mass spectrometry	Partial pressures, $CeO_2$ , $Ce_2O_3$	CeO <sub>1.99,</sub> Ce <sub>2</sub> O <sub>2.96</sub>	1900-2150 1850-2050	-
7.	Kuznetzov& Rezukhina (1960)	Calorimetry	Heat capacity,	CeO <sub>2</sub>	608-1172	-
8.	Westrum & Beale Jr. (1961)	Adiabatic Calorimetry	Heat capacity,	CeO <sub>2</sub>	5-300	+
9.	Justice & Westrum (1969)	Cryogenic Calorimetry	Heat capacity	Ce <sub>2</sub> O <sub>3.02</sub>	5-350	+
10.	Basily & El- Sharkawy (1979)	Plane temperature wave method	Heat capacity	Ce <sub>2</sub> O <sub>3</sub>	400-1000	+
11.	Ricken et al. (1984)	Calorimetry	Specific heat, $\Delta H_{trans.}$	CeO <sub>1.72</sub> - CeO <sub>2</sub>	320-1200	-
12.	Kuznetzov, et al. (1960)	Bomb calorimetry	$\Delta H$ for $Ce_2O_3$	Ce <sub>2</sub> O <sub>3.00</sub>	298	+

13.	Baker & Holley (1968)	Oxygen Bomb Calorimetry	Heat of combustion $Ce_2O_3$	Ce <sub>2</sub> O <sub>3</sub>	298.15	-
14.	Baker, Huber, Holley & Krikorian (1971)	Bomb calorimetry	Heat of formation $CeO_2, CeC_{1.5},$ $CeC_2$	CeO <sub>2</sub>	298.15	-
15.	Campserveux & Gerdanian (1974)	Micro Calorimetry	Partial molal enthalpy $\Delta H_{soln.}(O_2)$	CeO <sub>1.5</sub> - CeO <sub>2</sub>	1353	+
16.	Panlener, Blementhal & Garnier(1975)	Thermo- gravimetry	$\Delta W/W$	CeO <sub>2-x</sub>	1023-1773	+
17	Riess, Koerner & Noelting (1988)	Dilatometry	Thermal expansion coefficient	CeO <sub>1.79</sub> – CeO <sub>2</sub>	320-1200	+

# Calculated Ce–O System in Solid State from 60 to 67 mol. % O in comparison with experimental data.









H.J. Seifert, P. Nerikar, H.L. Lukas, Int. J. Mater. Res. 97 [6] (2006) 744-752.



## Chemical potentials of oxygen for ceria as a function of composition and temperature.







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#### Chemical potentials of oxygen for ceria as a function of composition and temperature.





Chemical potentials of oxygen for ceria as a function of composition and temperature.

#### Chemical potentials of oxygen in the two-phase areas.



#### **Partial Enthalpies of Oxygen in CeO<sub>2</sub>**



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**Precursor-derived Si-B-C-N Ceramics** 

- Produced by thermolysis (1323 K, Ar) of polymer precursors
- Amorphous, purely homogeneous inorganic materials
- NCP200: 40.1Si 23C 36.9N (at.%)
  - Starts to crystallize at 1700 K  $(N_2)$
  - Thermal stability up to 1800 K  $\left(N_{2}\right)$
- T2-1: 29.1Si 41.7C 19.4N 9.8B (at.%)
  - X-ray amorphous, nanocrystalline
  - Thermal stability up to 2300 K

#### **Process for Precursor-derived Si-(B-)C-N Ceramics**



#### Si-C binary subsystem



J. Gröbner, PhD thesis, 1994

#### Si-N binary subsystem







#### Isopleth from Carbon to Si<sub>3</sub>N<sub>4</sub> in the Si-C-N System



#### **Isothermal Section of the Ternary System Si-C-N**



#### **Isothermal Sections of the Ternary System Si-C-N**

- $\land$  Si<sub>1</sub>N<sub>1.6</sub>C<sub>1.33</sub> (VT50, Polyvinysilazane, Hoechst AG, Frankfurt, Germany)
- $Si_1N_{0.6}C_{1.02}$  (NCP200, Polyhydridomethylsilazane, Nichimen Corp., Tokyo, Japan)



Calculated Phase Fraction Diagrams of Precursor Derived Ceramics

 $Si_1N_{1.6}C_{1.33}$  $Si_3N_4 + 3C = 3SiC + 2N_2$ **(VT50)** 80  $Si_3N_4$ 1484°C 70 SiC 
Rel. Phase-Amount [Mass-%]

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Thermogravimetrical (TG) analysis of precursor-derived Si-C-N ceramics



#### Calculated Phase Fraction Diagram of Precursor Derived Ceramics

#### NCP200, Polyhydridomethylsilazane (Nichimen Corp., Tokyo, Japan)



**Phase Fraction Diagram** 



Thermogravimetrical (TG) analysis of precursor-derived Si-C-N ceramics



#### Thermogravimetrical (TG) analysis of precursor-derived Si-B-C-N ceramics







#### **Isothermal Section at 1500 K in the Ternary System Si-B-C**





#### Calculated Potential Phase Diagram



#### Calculated Potential Phase Diagram



#### Carbon activity - temperature diagram





#### Isopleth from B to $Si_1C_{1.6}N_{1.33}$ (VT50) in the Si-B-C-N System



# Isopleth from $B_{0.1}C_{0.65}Si_{0.25}$ to $B_{0.1}N_{0.65}Si_{0.25}$ in the Si-B-C-N System (at 10 mol-% B and 25 mol-% Si)





→ X (Si)





# Si-B-C-N concentration tetrahedron with indicated plane at a constant B content of 25 at.%





#### Isothermal Section at 10 mol-% B in the Si-B-C-N System



#### Isothermal Sections at 10 mol-% B in the Si-B-C-N System



#### System Si-B-C-N - Metastable phase separation -



